



Graph-Query Suggestions for Knowledge Graph Exploration

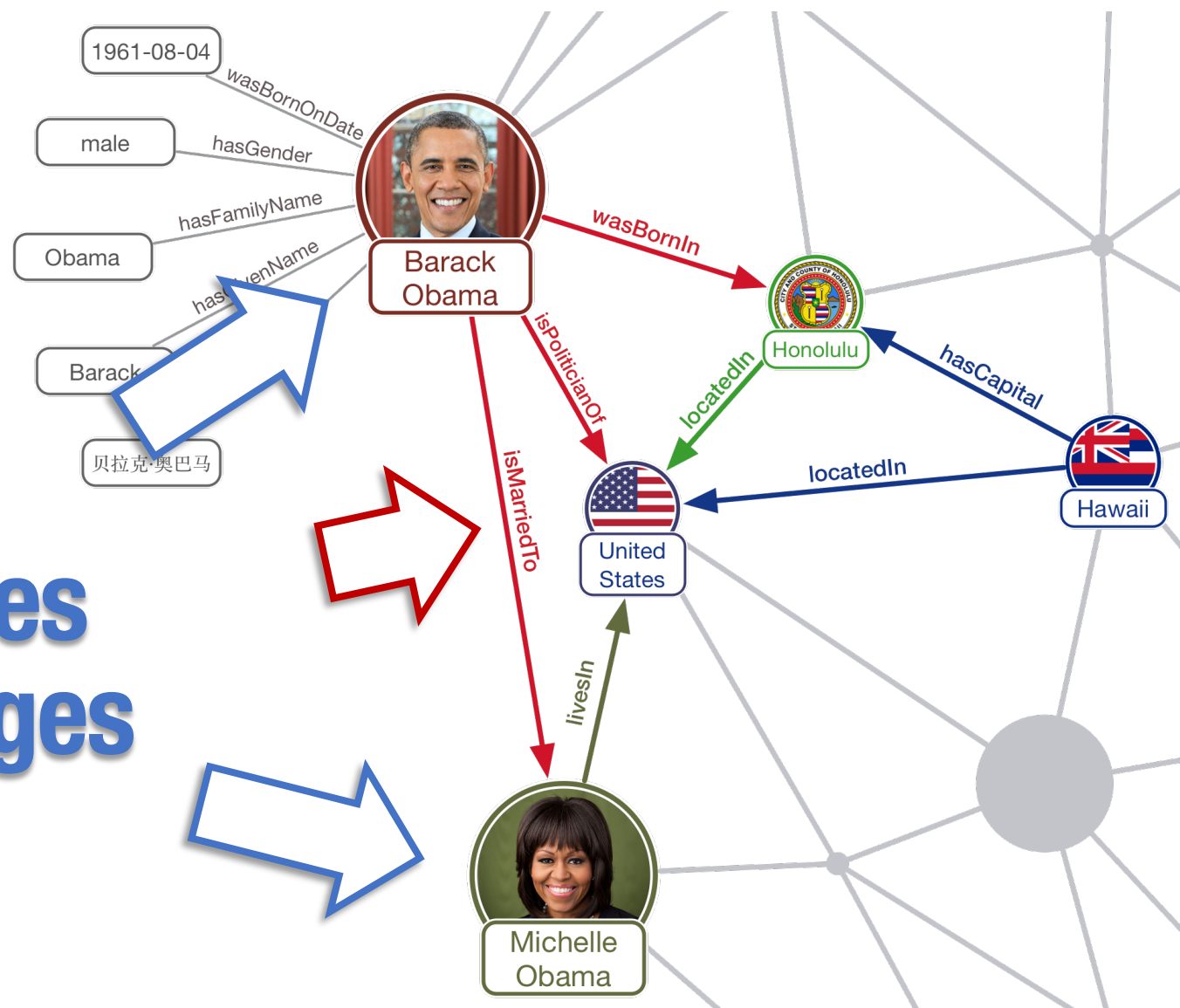
Matteo Lissandrini, Davide Mottin, Themis Palpanas, Yannis Velegrakis



Edge-labelled Multigraphs

$G: \langle V, E, L, \ell \rangle$

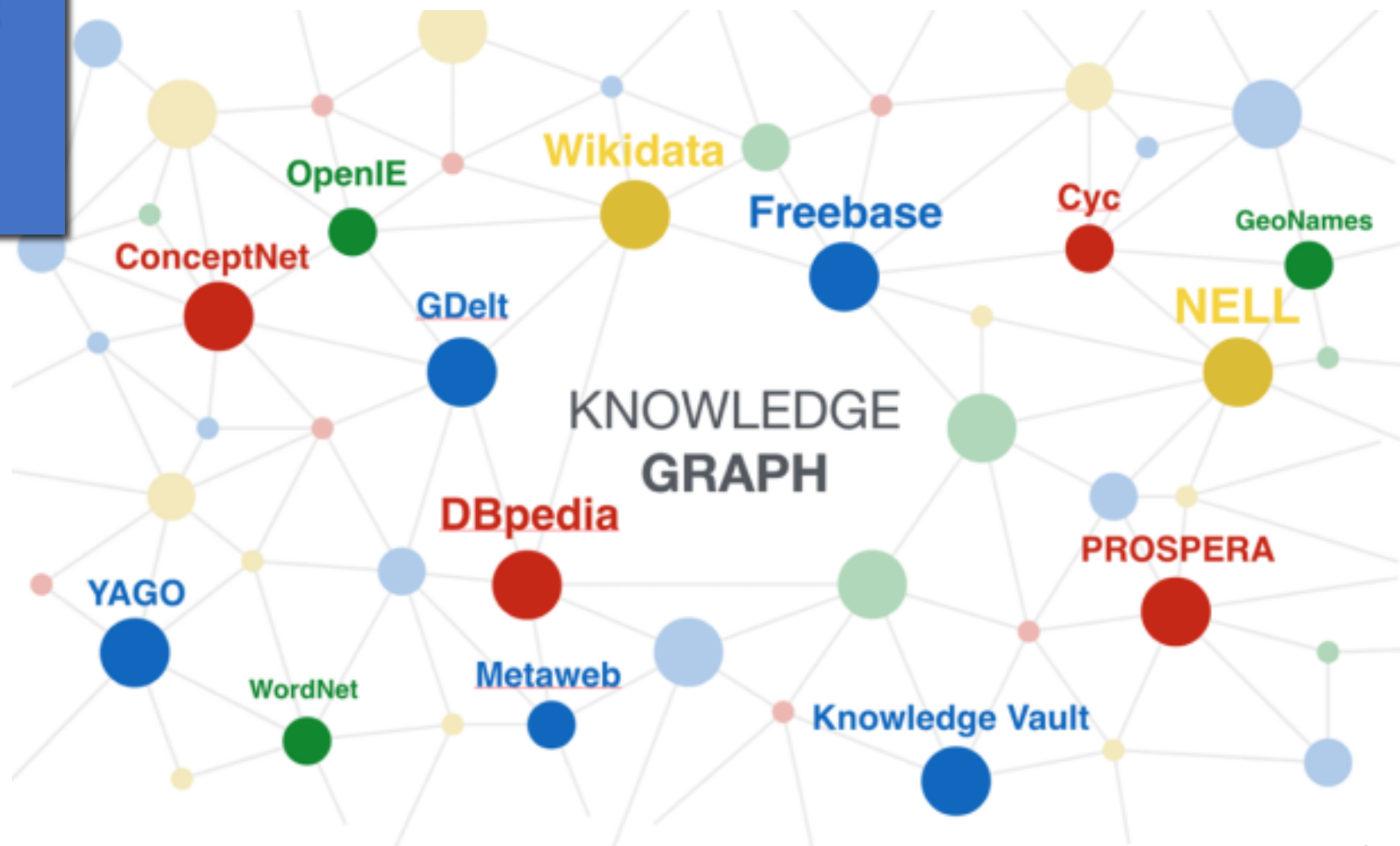
Nodes & Edges



Edge-labelled Multigraphs

$$G: \langle V, E, L, \ell \rangle$$

In use at:*



Exploration

500+ outgoing relationships

41 Edge Types

ing point"

edge

complex

Nietzsche

Kierkegaard

Schopenh

Herac

Thomas Paine

J.J. Rousseau

Auguste Comte

Michel de Montaigne

Max Stirner

William Hazlitt

Chris Bateman

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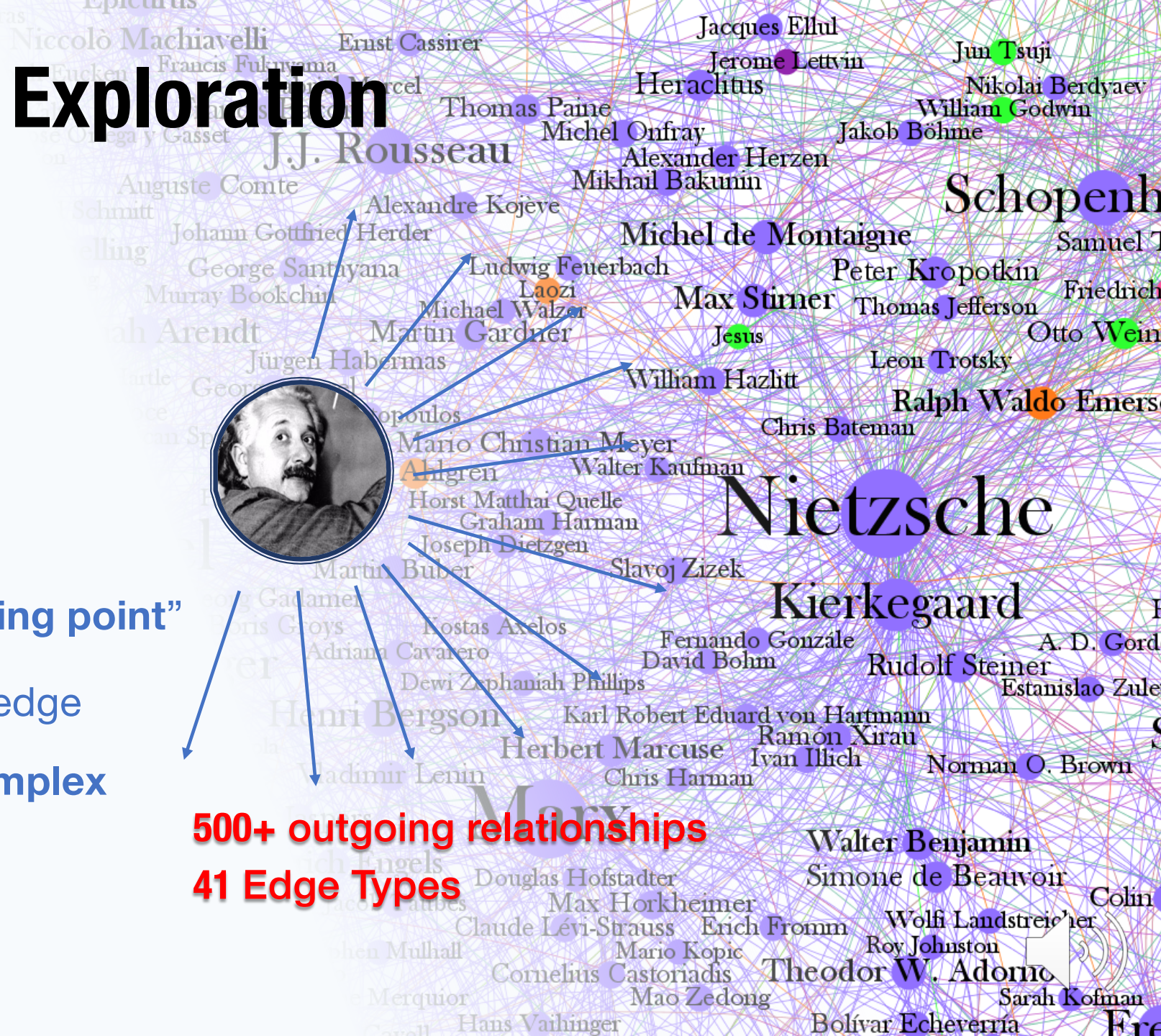
Jacob Böhme

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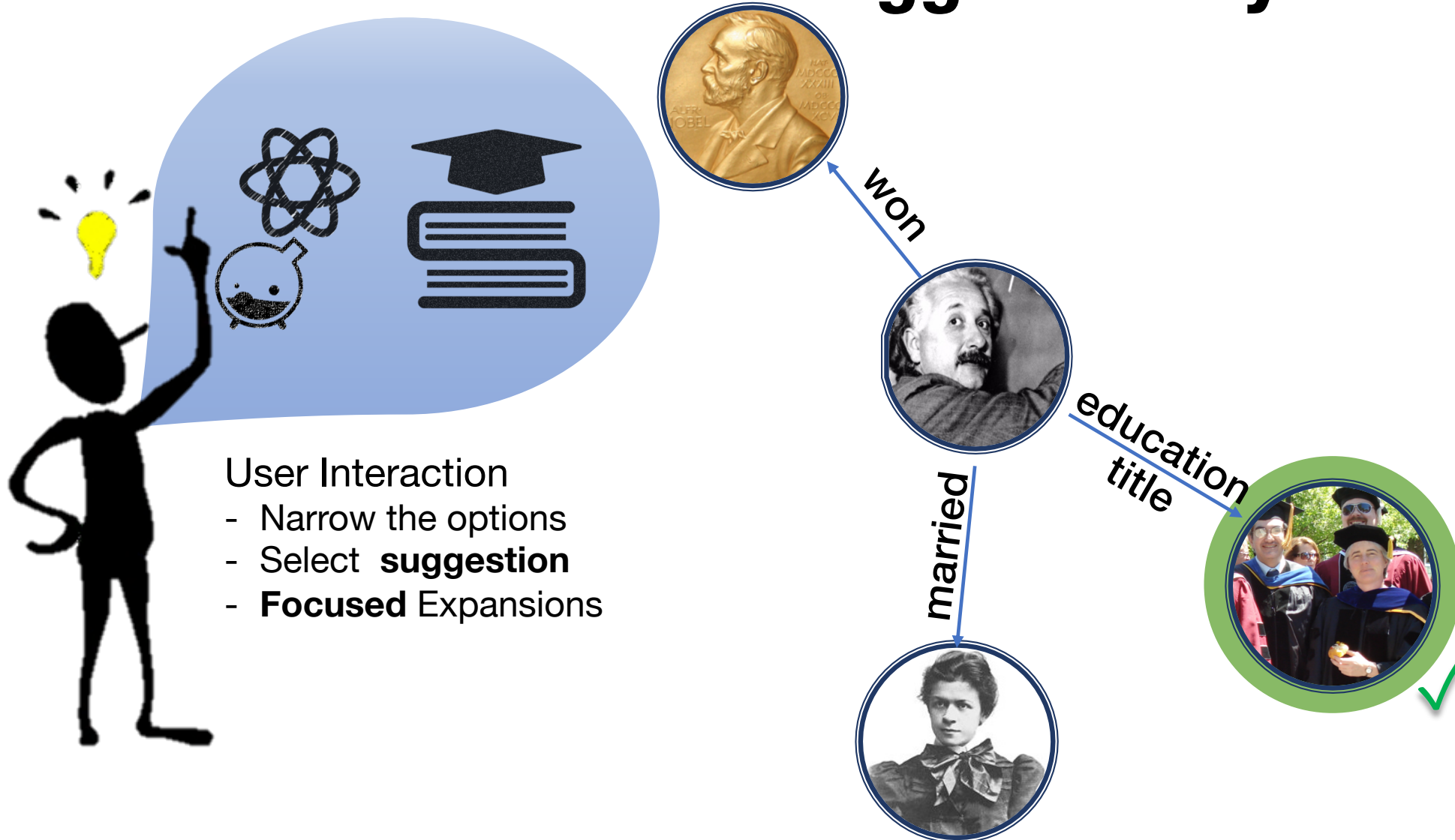
Niccolò Machiavelli</



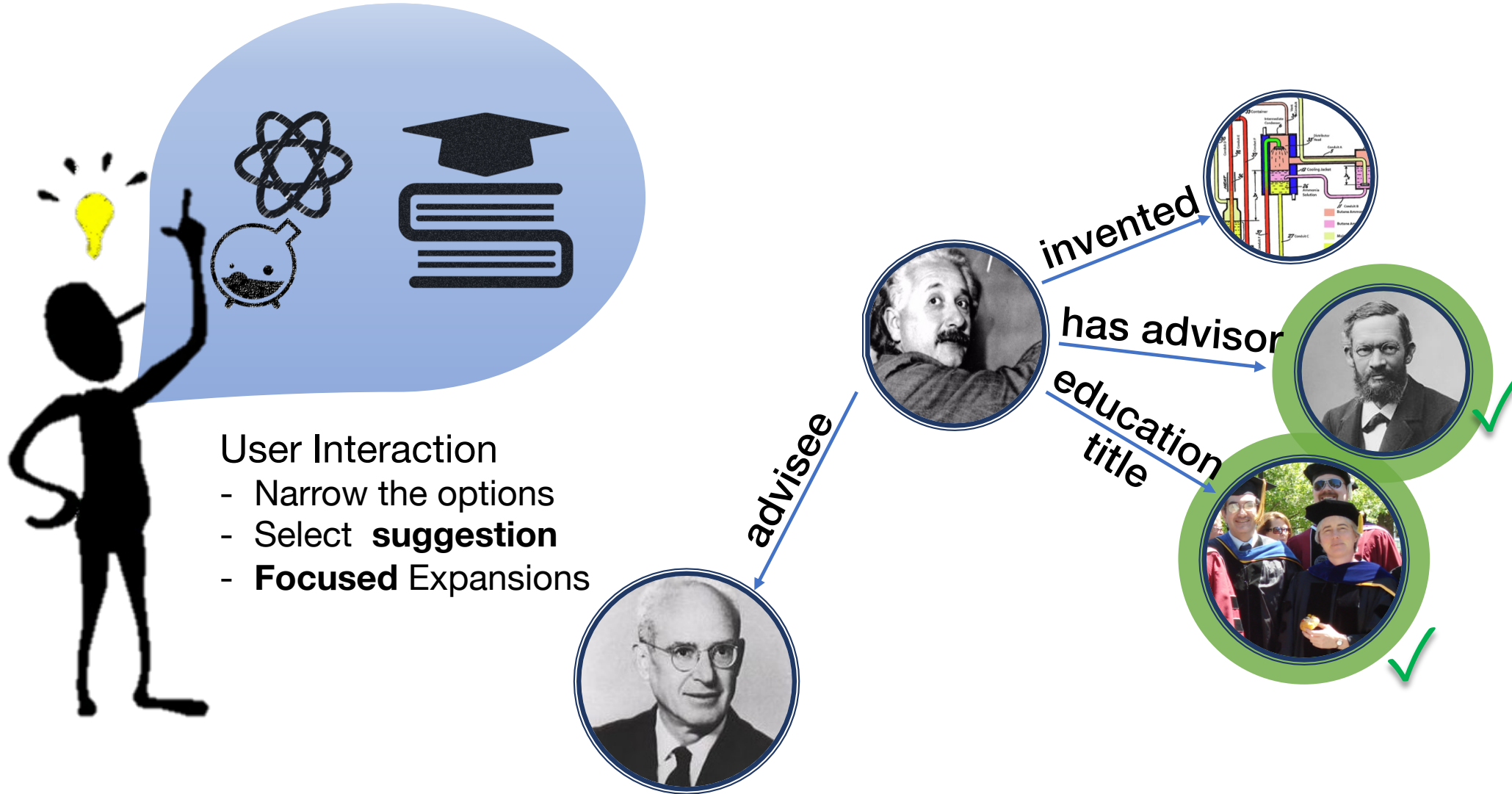
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- Exploration**
- 500+ outgoing relationships**
- 41 Edge Types**

[illegible]

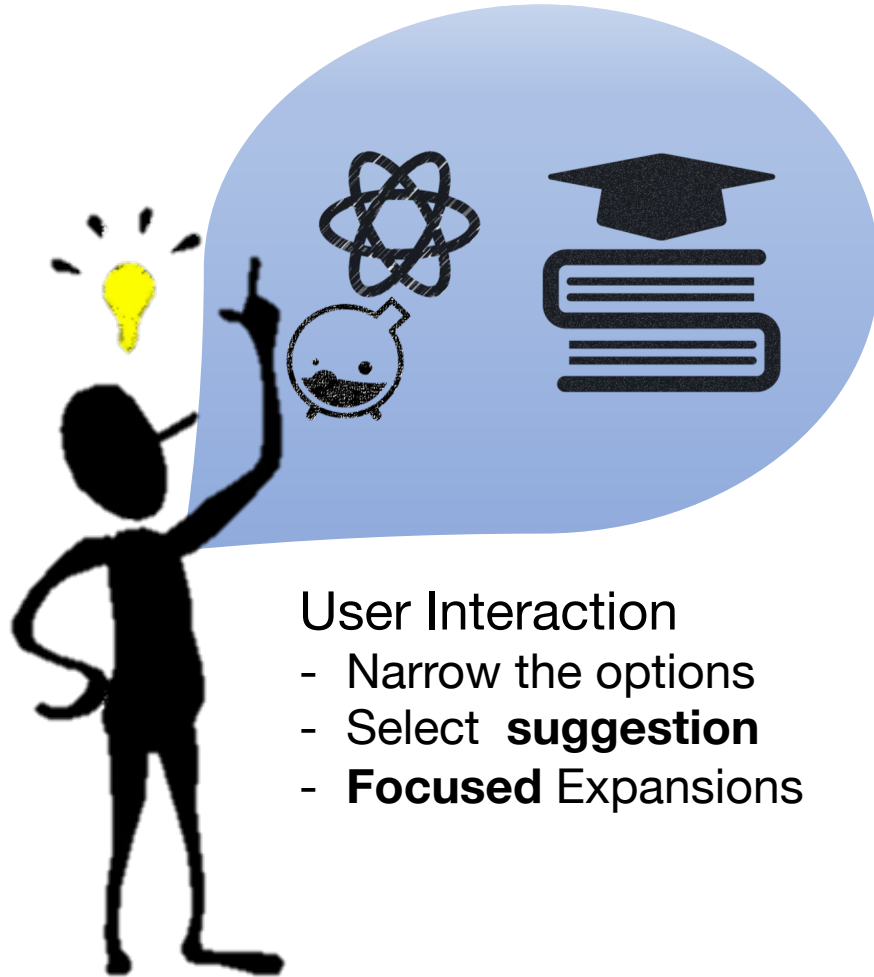
Solution: **Interactive Suggestion System**



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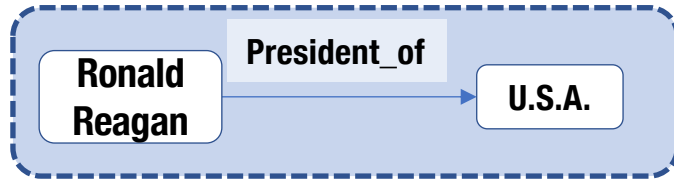
User Interaction

- Narrow the options
- Select **suggestion**
- **Focused** Expansions

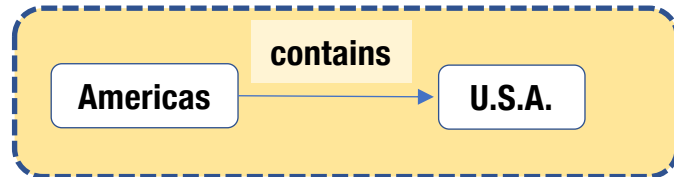


Suggesting Expansions

The User Search

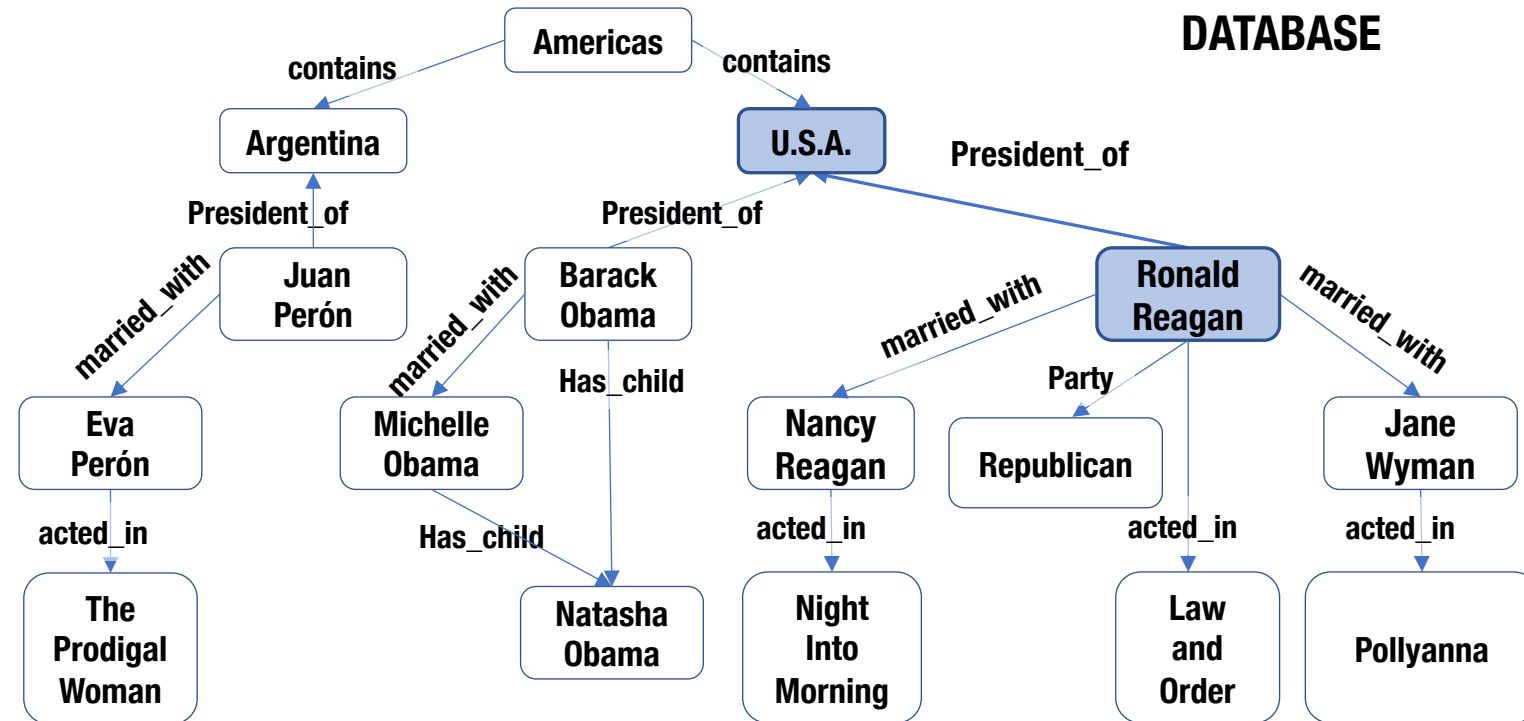


Which Expansion to Suggest?



...

Rank Expansions

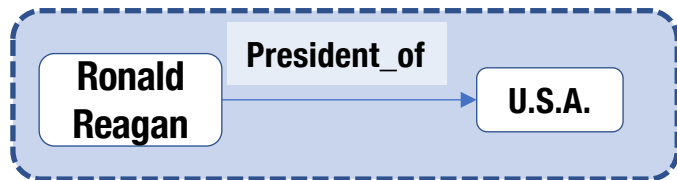


Approach:
Rank Edges based
on Label characteristics

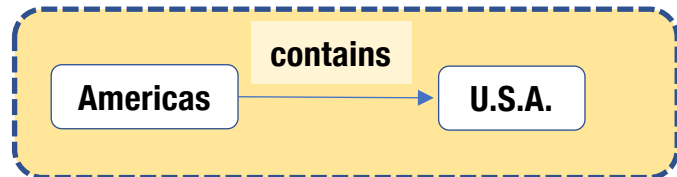
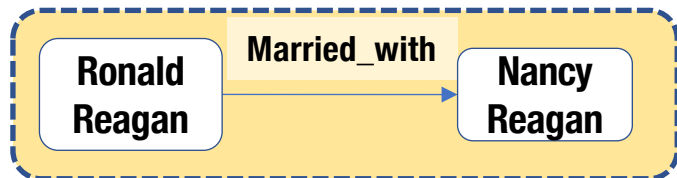


Suggesting Expansions: **Ranking Labels (I)**

The User Search



How to score Expansions?



Baseline Methods: Language Model

1. **Frequent** in the Graph
2. **Frequent** Around the Query

Probabilistic Model
for the Query

$$\hat{p}(l|M_{\bar{Q}})_{MLE} = \frac{|E_Q^l| + \epsilon \hat{p}(l|\mathcal{K})}{|E_Q| + \epsilon}$$

3. **Frequent** Around the Query but **Infrequent** in the Graph

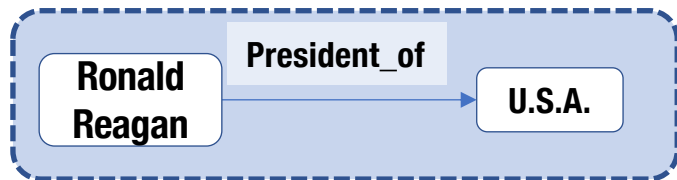
Kullback–Leibler
divergence

$$\hat{p}(l|M_{\bar{Q}})_{KL} \propto \exp \left(\frac{1}{(1-\lambda)} \log (\hat{p}(l|M_{\bar{Q}})) - \frac{\lambda}{(1-\lambda)} \log (\hat{p}(l|\mathcal{K})) \right)$$



Suggesting Expansions: **Ranking Labels (I)**

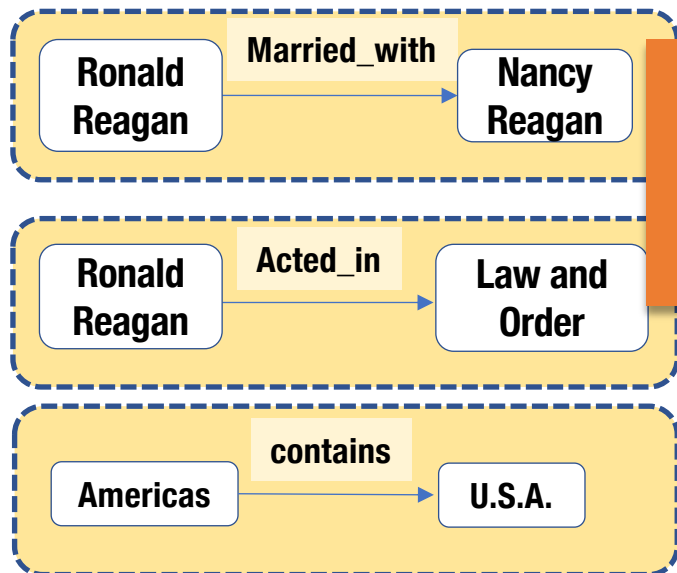
The User Search



Baseline Methods: Language Model

1. **Frequent** in the Graph
2. **Frequent** Around the Query

How to score Expansions?



Probabilistic Model

LIMITED INFORMATION

Looks only around the query + Global information

Kullback–Leibler divergence

$$\hat{p}(l|M_{\bar{Q}})_{KL} \propto$$

$$\exp \left(\frac{1}{(1-\lambda)} \log (\hat{p}(l|M_{\bar{Q}})) - \frac{\lambda}{(1-\lambda)} \log (\hat{p}(l|\mathcal{K})) \right)$$

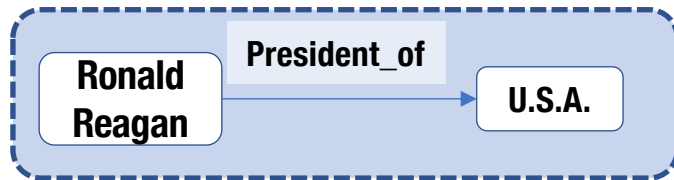
$$\frac{|E_O^l| + \epsilon \hat{p}(l|\mathcal{K})}{|E_Q| + \epsilon}$$

but **Infrequent** in the Graph

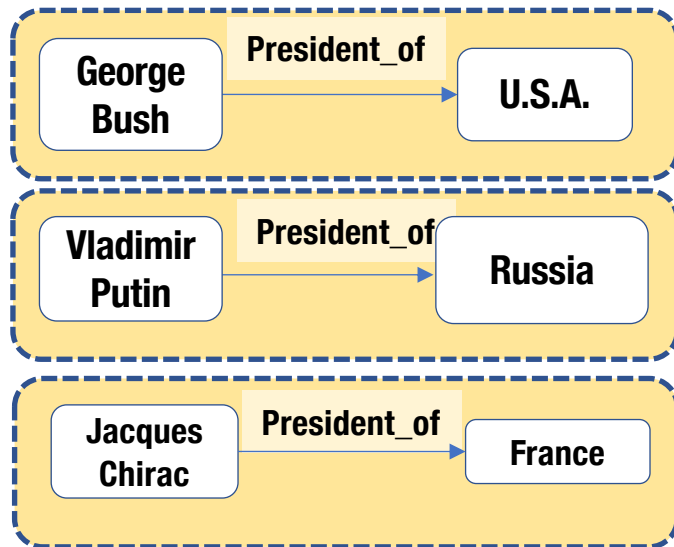


Suggesting Expansions: **Ranking Labels (II)**

The User Query Q



The result-set R



Intuition:
Exploit Classical IR Model

Pseudo Relevance Feedback

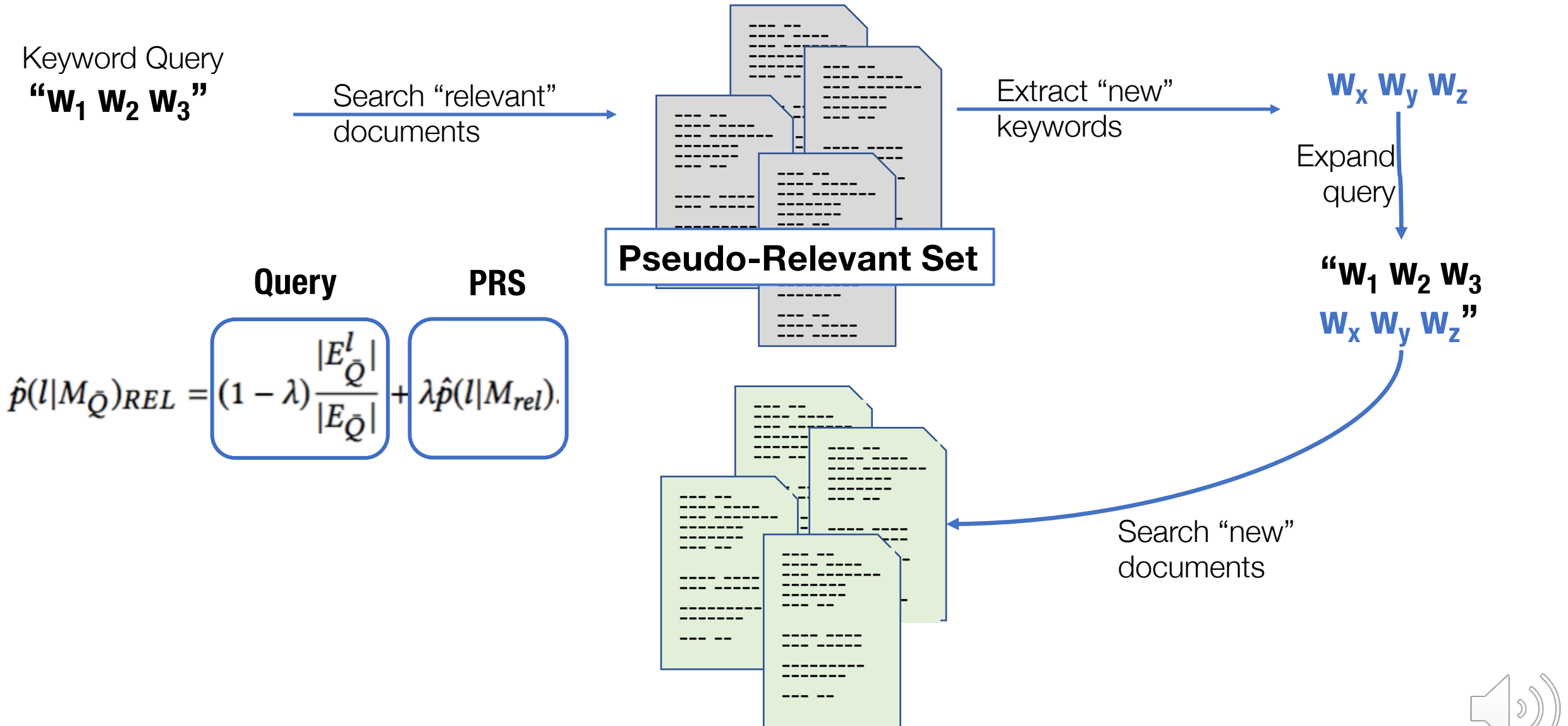
1. **Retrieve** “similar” elements **R**,
resolve user query – e.g., Top-K ExQ Search

Pseudo-Relevant Set

2. **Compute** statistics about **R**
& use to **score** expansions



Pseudo Relevance Feedback for Document Search



Pseudo Relevance Feedback Models

Maximum Likelihood Estimation

$$\hat{p}(l|M_{rel})_{MLE} \approx \sum_{\bar{G} \in \bar{\mathcal{G}}_{rel}} \hat{p}(l|M_{\bar{G}}) \hat{p}(\bar{Q}|M_{\bar{G}})$$

$$\hat{p}(\bar{Q}|M_{\bar{G}}) \propto \prod_{l \in \bar{Q}} \hat{p}(l|M_{\bar{G}})$$

PRS

$$\hat{p}(l|M_{\bar{Q}})_{REL} = (1 - \lambda) \frac{|E_{\bar{Q}}^l|}{|E_{\bar{Q}}|} + \lambda \hat{p}(l|M_{rel}).$$

2 Models of Estimation MLE & KL-Divergence

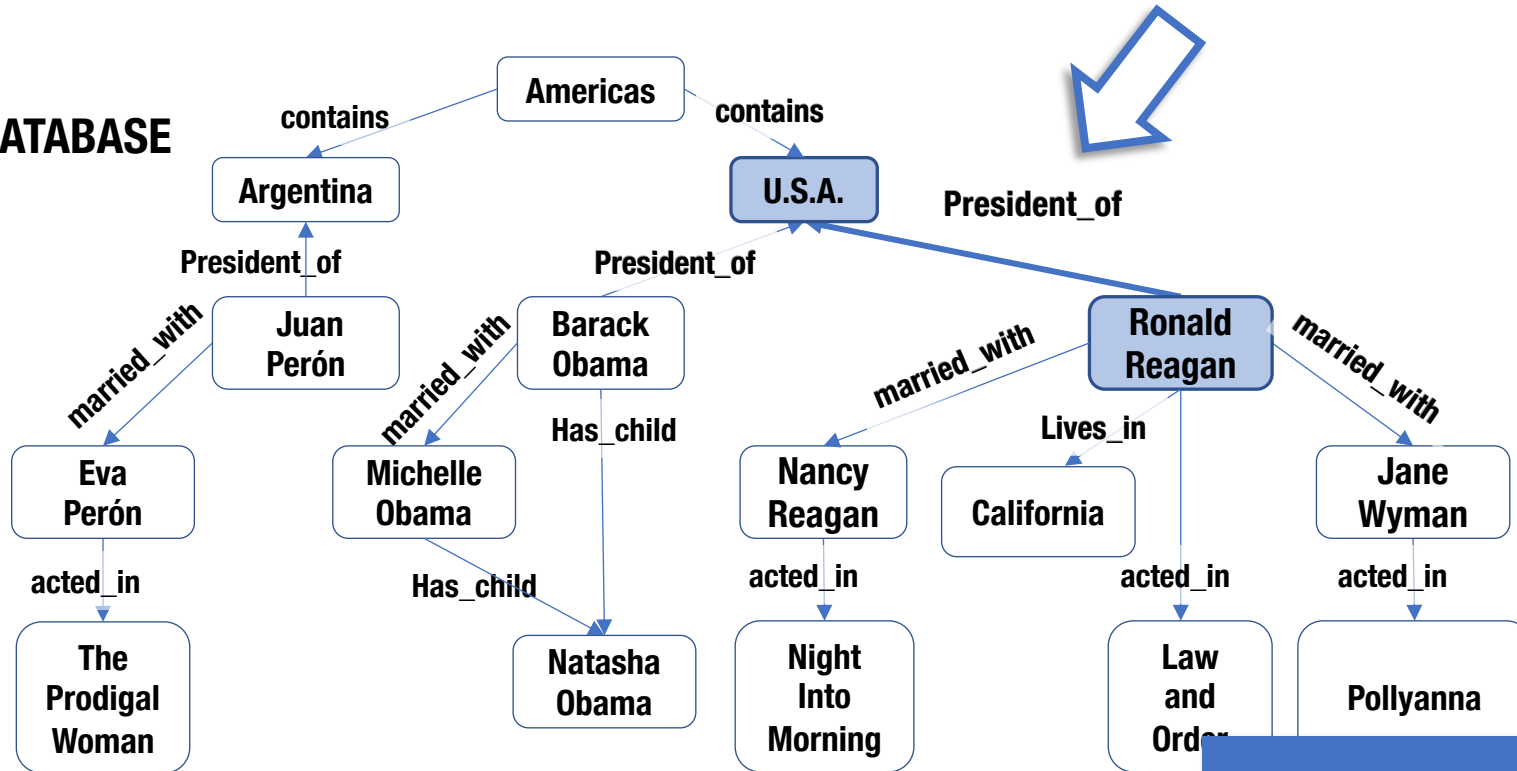
KL-Divergence

$$\hat{p}(l|M_{rel})_{KL} \propto \exp \left(\frac{1}{(1 - \lambda)} \frac{1}{|\bar{\mathcal{G}}_{rel}|} \sum_{\bar{G}}^{\bar{\mathcal{G}}_{rel}} \log(\hat{p}(l|M_{\bar{G}})) - \frac{\lambda}{(1 - \lambda)} \log(\hat{p}(l|\mathcal{K})) \right)$$

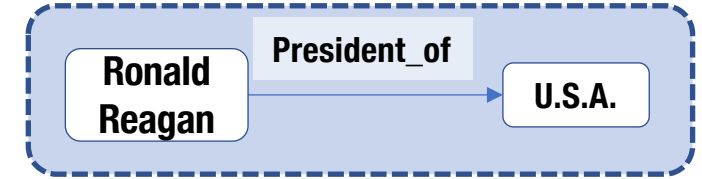


Bag Model for Graphs

DATABASE



The User Search



How can we convert to the document model?

The Bag-of-Labels Model

President_of, contains, married_with, married_with, acted_in, lives_in

- Graphs can be modeled as **Bag of Words**
- Describes **MORE** than what is in the query



Graph Query Suggestion Framework

Steps:

- Decide the **scoring model**
(Query & PR-Set)
- **Transform** query into Bag of Labels
(obtain candidate expansions)
- Compute **Scoring Model**
- **Score expansions**
- Return top-k expansions

Expansions can be **EDGES**
or **LABELS**

Algorithm 1 Graph-Query Suggestion

Input: Knowledge graph $\mathcal{K} : \langle V, E, \ell \rangle$

Input: Current query $Q : \langle V_Q, E_Q, \ell \rangle$

Input: Current answers \mathcal{A}_Q

Input: Model M \triangleright One defined by Eq 1, 2, 4, 5, or 7

Input: Number of expansions k

Output: Expansions $\langle l_1, l_2, \dots, l_k \rangle$

1: $E_\varepsilon \leftarrow \emptyset$

2: **for each** $v_i \in V_Q$ **do**

3: $E_\varepsilon \leftarrow E_\varepsilon \cup \text{GETEDGES}(v, E)$

4: $E_\varepsilon \leftarrow E_\varepsilon \setminus E_Q$

5: $L_\varepsilon \leftarrow \{\ell(e) | e \in E_\varepsilon\}$

6: $\text{ESTIMATEMODEL}(M, E_\varepsilon, L_\varepsilon, \mathcal{A}_Q)$

7: $\text{Scores} \leftarrow \text{new Dict}()$

8: **for each** $l \in L_\varepsilon$ **do**

9: $\text{Scores} \leftarrow \{l : \rho_M(Q, l)\}$

10: $\text{Scores} \leftarrow \text{sort}(\text{Scores})$

11: **return** $\text{Scores.get}(k)$



Experimental Evaluation (I)

5 Ranking Scores:

- a) **Based on the Query Alone**
 - **Maximum Likelihood Estimation (MLE)**
 - **Kullback–Leibler divergence (KL)**
- b) **Based on the PR-Set**
 - **Maximum Likelihood Estimation (MLE-rel)**
 - **Kullback–Leibler divergence (KL-rel)**
 - **“Surprise” heuristics (Srp)** [[Sarkas et al.'09](#)]

Baselines:

- **Random**
- **Personalized Page Rank**
- **Distant supervision** [[N.Voskarides, et al.'18](#)]

Real Dataset: Freebase +300M Edges

Tests (compare NDCG):

- **65 Queries from QUALD-7 benchmark**
Contain 1 entity, 1 edge, 2+ edges
- **KG-contextualization Dataset** [[N.Voskarides, et al.'18](#)]

Example query: “doctoral supervisor, Albert Einstein”

- *Mapped to:*
 - *Single Entity: Albert Einstein*
 - *Edge: <Albert Einstein, advisor, A, Kleiner >*
- *Described with general topic*
 - *“Academic Information of Albert Einstein”*



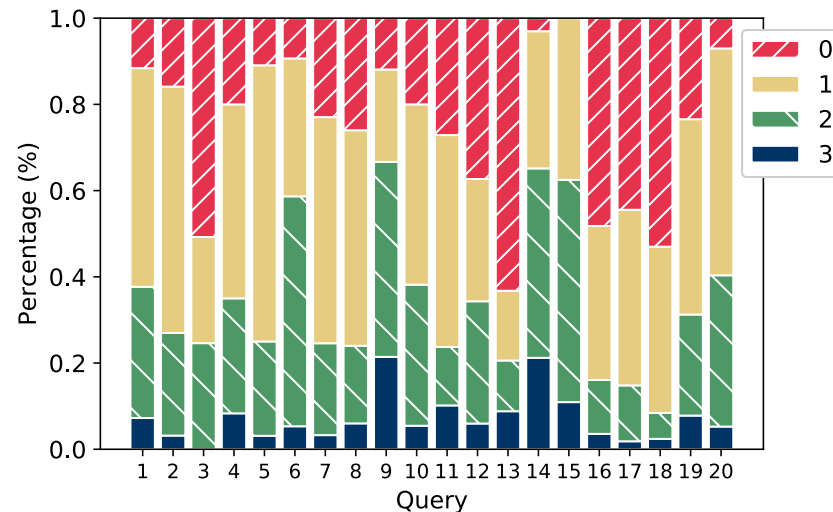
Experimental Evaluation (II)

65 Queries from QUALD-7 benchmark - Contain 1 entity, 1 edge, 2+ edges

For Each Query (graph+description)
& Each Method → Produce 20 Query expansions



Ask 3 Human judges* to evaluate relatedness of each suggestion
irrelevant (0), uninteresting (1), fairly interesting (2), really interesting (3)

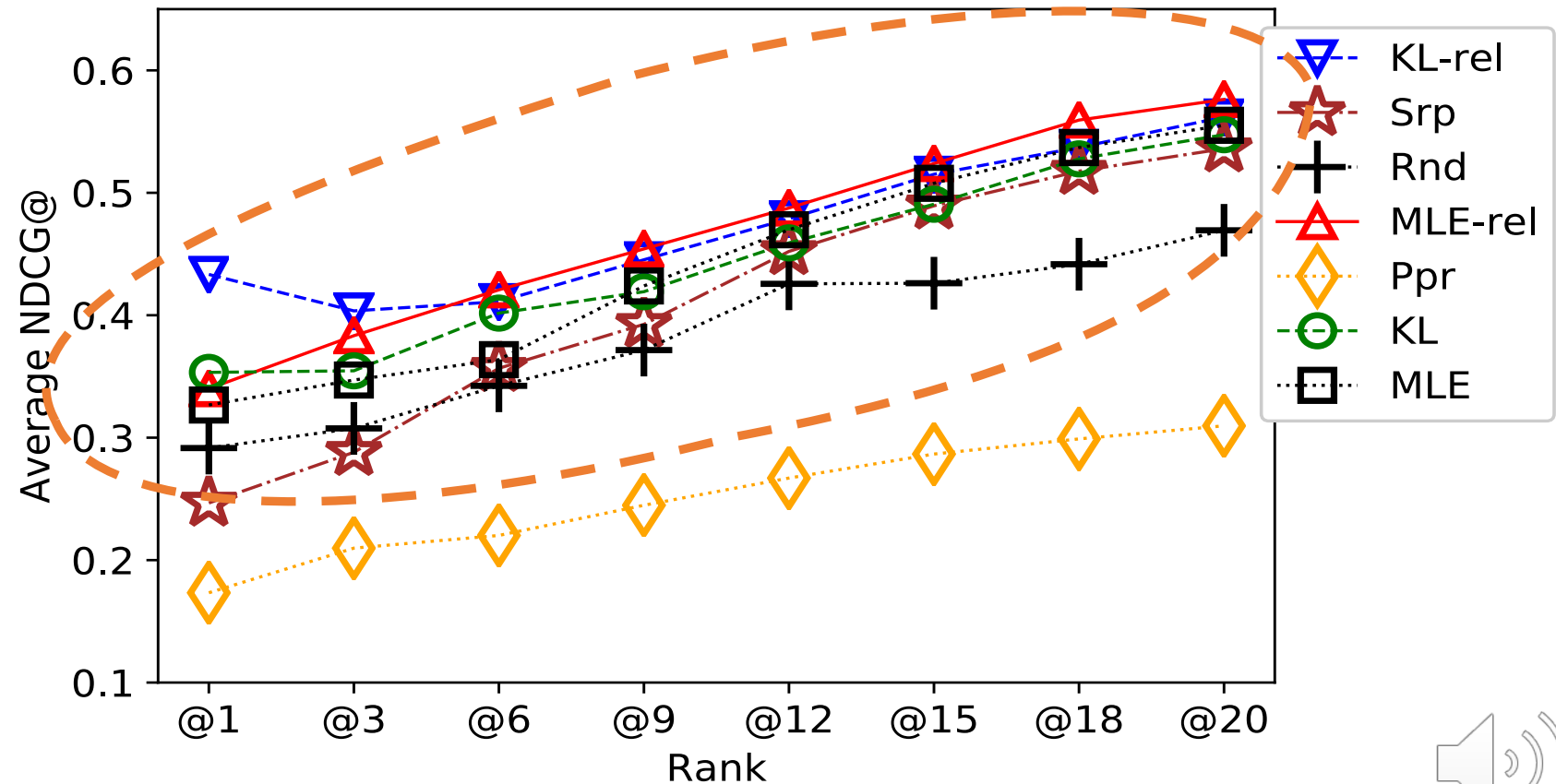


Among all rankings
Few Expansion per Query
were considered fairly interesting



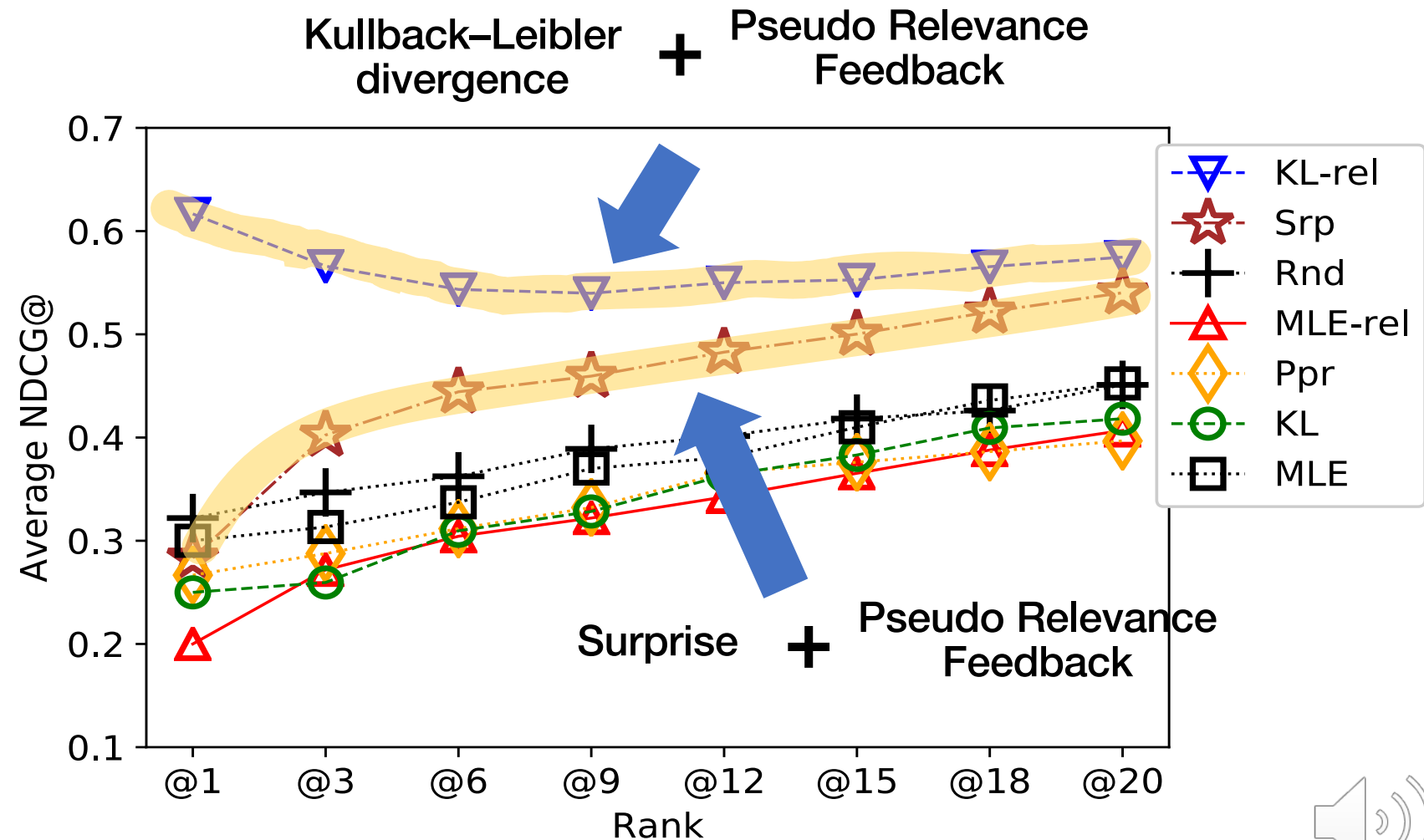
Evaluation Results: Suggestions with 1 Entity

**With 1 Entity
we can only guess**



Evaluation Results: Suggestions with 1 Edge

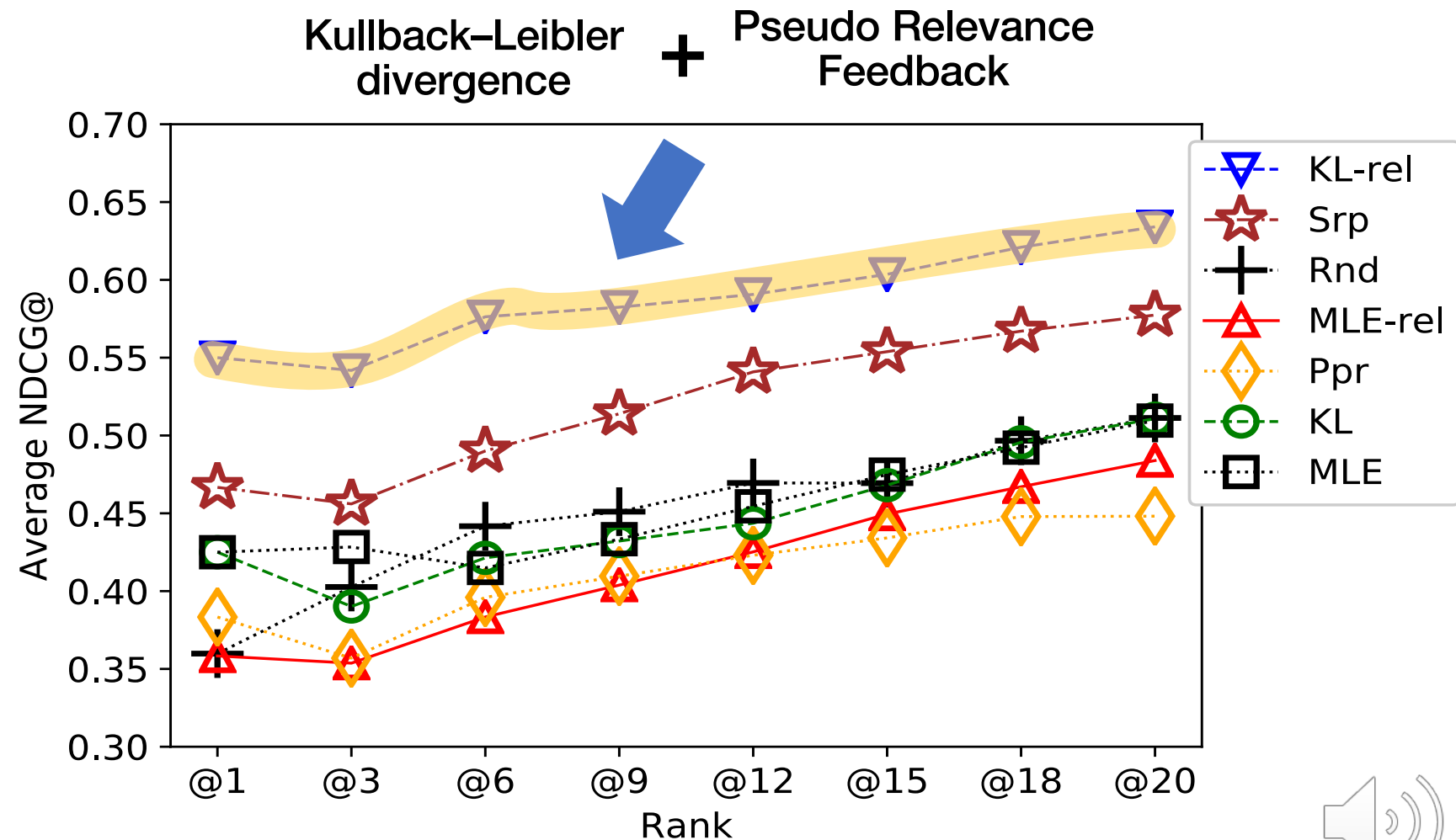
**With 1 Edge
Precision
Drastically increases**



Evaluation Results: Suggestions with 2+ Edges

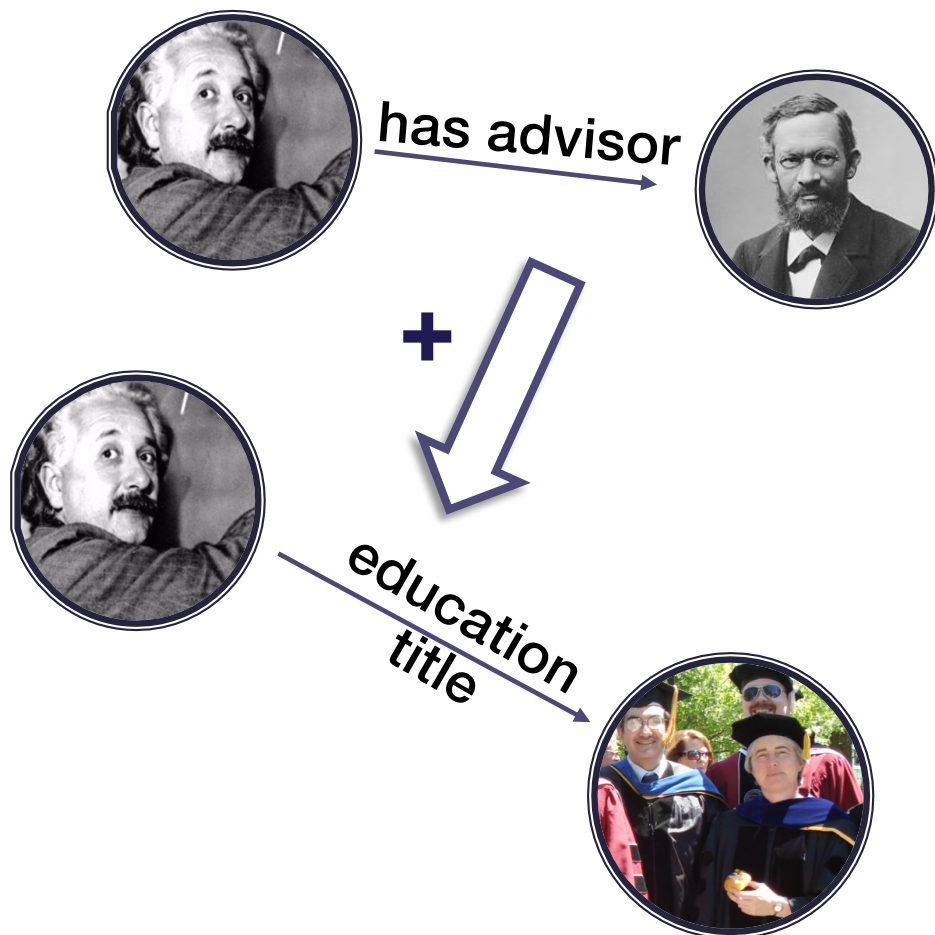
**With 2+ Edges
KL-rel does not suffer
any loss in precision**

With more edges in the query
the number of alternatives
increases



KG Query Suggestion

Given a Graph Query suggest query expansions



Summary

Guide the User in Exploring a KG with complex and rich schema.

The Bag-of-Labels model provide and expressive model for Graph Queries on KGs

1. Exploit State-of-the-Art IR query suggestion techniques
2. Bridge Structural-queries and Semantic of relationship
3. Provide effective Ranking with just 1 edge
4. Does not require pre-training of ML models
5. Can be expanded with more complex ranking models

<http://j.mp/WebConfKG>

