# Simulation-Based Admissible Dominance Pruning 

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## Motivation

- Cost-optimal planning: $(\mathcal{V}, \mathcal{O}, \mathcal{I}, \mathcal{G})$
- $\mathrm{A}^{*}+$ admissible heuristic $\mathrm{h}(\mathrm{s})$ : estimates distance to goal
- Pruning methods:
(1) Partial-order pruning
(2) Symmetries
(3) Dominance pruning


## Dominance Pruning



I'm
Happy


I'm
okay


I'm
sad

## Dominance Pruning

- Detect "better than" states


$$
\begin{aligned}
\mathcal{V}= & \{\text { at }-T=\{A, B\}, \text { at }-P=\{A, B, T\}\} \\
\mathcal{I}= & \{\text { at-T } A, \text { at-P } A\} \\
\mathcal{G}= & \{\text { at }-P B\} \\
\mathcal{O}= & \{\text { move }-T(A, B), \\
& \text { move }-T(B, A), \operatorname{load}-P(A), \ldots\}
\end{aligned}
$$

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- What do you prefer?



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\mathcal{G}= & \{\text { at }-\mathrm{P} B\} \\
\mathcal{O}= & \{\operatorname{move}-\mathrm{T}(\mathrm{~A}, \mathrm{~B}), \\
& \text { move }-\mathrm{T}(\mathrm{~B}, \mathrm{~A}), \operatorname{load}-\mathrm{P}(\mathrm{~A}), \ldots\}
\end{aligned}
$$

- What do you prefer?

- Formally: relation of pair of states $s \preceq t$


## Admissible Pruning

- $t$ simulates $s(s \preceq t) \Longrightarrow t$ is at least as good as $s$ :

$$
h^{*}(s) \geq h^{*}(t)
$$

- If $g(t) \leq g(s)$ and $s \preceq t$ then $s$ can be discarded



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$$
\begin{gathered}
s_{1} \preceq s_{3} \\
s_{1}
\end{gathered}
$$



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Challenges:
(1) How to find good dominance relations?
(2) How to efficiently check dominance?

## Simulation Relation

## Definition (Simulation)

A binary relation $\preceq \subseteq S \times S$ is a simulation for $\Theta$ if, whenever $s \preceq t$, for every transition $s \xrightarrow{\prime} s^{\prime}$ there exists $t \xrightarrow{\prime} t^{\prime}$ s.t. $s^{\prime} \preceq t^{\prime}$. We call $\preceq$ goal-respecting for $\Theta$ if, whenever $s \preceq t, s \in S_{G}$ implies that $t \in S_{G}$.

$D \preceq B$
Thm: A unique coarsest goal-respecting simulation always exists and can be computed in time polynomial in the size of $\Theta$

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Cost-simulation: replace labels by their cost
$\rightarrow$ A cost-simulation on the state space of the planning task is a dominance relation

Thm: A unique coarsest goal-respecting simulation always exists and can be computed in time polynomial in the size of $\Theta$

## Compositional Approach

(1) Consider a partition of the problem: $\Theta_{1}, \ldots, \Theta_{k}$
(2) Compute a simulation for each part: $\preceq_{1}, \ldots, \preceq_{k}$
(3) $\preceq: s \preceq t$ iff $\forall i \in[1, k] s_{i} \preceq_{i} t_{i}$
$\preceq$ is a cost-simulation

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In our example:
$\Theta^{1}:$
(truck)
$\Theta^{2}:$
(package)


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## Not so fast

Definition of $s \preceq t$ : For every $s{ }^{\prime} s^{\prime}$ there exists $t \xrightarrow{\prime} t^{\prime}$ s.t. $s^{\prime} \preceq t^{\prime}$

(truck)
$\Theta^{2}$ :
(package)


$$
A \preceq_{2} T \preceq_{2} B
$$

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$T \xrightarrow{I B} B$ and $T \xrightarrow{I A} A$ are simulated by $B \rightarrow$

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$T 九_{2} B: T \xrightarrow{I B} B$ and there is no $B \xrightarrow{I B}$
$T \xrightarrow{I B} B$ and $T \xrightarrow{I A} A$ are simulated by $B \xrightarrow{\text { noop }} B$
$I A, I B$ do not have useful effects in the rest of the problem $\left(\Theta^{1}\right)!$

## Label-Dominance Simulation

## Definition (Label Dominance)

$I^{\prime}$ dominates $/$ in $\Theta$ given $\preceq$ if for every $s \xrightarrow{\prime} s^{\prime} \in \Theta$ there exists $s \xrightarrow{\prime \prime} t^{\prime}$ s.t. $s^{\prime} \preceq t^{\prime}$

## Definition (Label-Dominance Simulation)

A set $\mathcal{R}=\left\{\preceq_{1}, \ldots, \preceq_{k}\right\}$ of binary relations $\preceq_{i} \subseteq S_{i} \times S_{i}$ is a label-dominance simulation for $\left\{\Theta^{1}, \ldots, \Theta^{k}\right\}$ if, whenever $s \preceq_{i} t$ :

- $s \in S_{i}^{G}$ implies that $t \in S_{i}^{G}$
- For every $s \xrightarrow{\prime} s^{\prime}$ in $\Theta^{i}$, there exists $t \xrightarrow{\prime \prime} t^{\prime}$ in $\Theta^{i}$ s.t.:
(1) $s^{\prime} \varliminf_{i} t^{\prime}$,
(2) $c\left(I^{\prime}\right) \leq c(I)$, and
(3) for all $j \neq i, l^{\prime}$ dominates / in $\Theta^{j}$ given $\preceq_{j}$


## Label-Dominance Simulation: Theoretical Results

## Theorem <br> A coarsest label-dominance simulation always exists and can be computed in polynomial time

For all $i$, set $\preceq_{i}:=\left\{(s, t) \mid s, t \in S_{i}, s \notin S_{G}^{i}\right.$ or $\left.t \in S_{G}^{i}\right\}$
while ex. (i, s,t) s.t. not $\mathbf{O k}(i, s, t)$ do
Select one such triple ( $i, s, t$ )
Set $\preceq_{i}:=\preceq_{i} \backslash\{(s, t)\}$
return $\mathcal{R}:=\left\{\preceq_{1}, \ldots, \preceq_{k}\right\}$

## Theorem

Combination of $\left\{\preceq_{1}, \ldots, \preceq_{k}\right\}$ is a cost-simulation for the planning task $\Theta_{1} \otimes \cdots \otimes \Theta_{k}$

## Computation of Label-Dominance Simulation

$\Theta^{1}:$
(truck)

$\Theta^{2}:$
(package)


Truck

$$
\begin{aligned}
& \mathrm{A} \preceq_{1}\{\mathrm{~B}\} \\
& \mathrm{B} \preceq_{1}\{\mathrm{~A}\}
\end{aligned}
$$

Package

$$
\begin{aligned}
& \mathrm{A} \preceq_{2}\{\mathrm{~T}, \mathrm{~B}\} \\
& \mathrm{T} \preceq_{2}\{\mathrm{~A}, \mathrm{~B}\} \\
& \mathrm{B} \preceq_{2}\{ \}
\end{aligned}
$$

(noop $\equiv d r$ ) simulate $\{I A\}$ dr simulates $\{I A, I B\}$

## Computation of Label-Dominance Simulation



Truck

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noop simulates $\{I A, I B, d r\}$ $d r$ simulates $\{I A, \mid B\}$

## Computation of Label-Dominance Simulation



Truck

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(noop $\equiv d r$ ) simulate $\{\mid \mathrm{A}\}$
noop simulates $\{I A, I B$, dr $\}$ $d r$ simulates $\{I A, \mid B\}$

## Computation of Label-Dominance Simulation



Truck

$$
\begin{aligned}
& \mathrm{A} \preceq_{1}\{B\} \\
& \mathrm{B} \preceq_{1}\{\mathrm{~A}\}
\end{aligned}
$$

noop simulates $\{I A, I B, \mathrm{dr}\}$ $d r$ simulates $\{|\mathrm{A}| \mathrm{B}$,

Package

$$
\begin{aligned}
& \mathrm{A} \preceq_{2}\{\mathrm{~T}, \mathrm{~B}\} \\
& \mathrm{T} \preceq_{2}\{\mathrm{~A}, \mathrm{~B}\} \\
& \mathrm{B} \preceq_{2}\{ \}
\end{aligned}
$$

(noop $\equiv d r$ ) simulate $\{\mid \mathrm{A}\}$

## Pruning: Implementation Details

- Insert in closed every state dominated by any expanded state
$\rightarrow$ BDD $B_{g}$ represents any state expanded/dominated with $g$
- When $s$ is generated or expanded:
(1) Prune $s$ if it is in $B_{g^{\prime}}$ for some $g^{\prime} \leq g(s)$
- When $s$ is expanded:
(1) Insert all states dominated by $s$ in $B_{g(s)}$


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- When $s$ is generated or expanded:
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- When $s$ is expanded:
(1) Insert all states dominated by $s$ in $B_{g(s)}$
- Safety Belt: Stop if no state is pruned after 1000 expansions
- Don't waste time if no useful dominance relation has been found


## Experimental Results

- M\&S: Merge-DFP + bisimulation up to 100000 transitions
- Pruning types:
- A: Baseline without pruning
- L: Label-dominance simulation
- S: Simulation
- B: Bisimulation
- P: Partial-order reduction
- Heuristic: Blind or LM-cut


## Experimental Results: Blind Search

| Domain | \# | Coverage |  |  |  |  | Evaluations |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | A |  | S | B | P | L | S | B | P |
| Airport | 50 | 22 | -7 | -7 | 0 | -1 | 1.2 | 1.2 | 1 | 4.4 |
| Driverlog | 20 | 7 | +2 | 0 | 0 | 0 | 15.8 | 2 | 2 | 1 |
| Floortile11 | 20 | 2 | +4 | +4 | 0 | 0 | 177 | 177 | 1.8 | 1.3 |
| Gripper | 20 | 8 | +6 | +6 | +6 | , | 53968 | 53968 | 28353 | 1 |
| Logistics00 | 28 | 10 | +6 | 0 |  | 0 | 32.7 | 3.1 | 1.2 | 1 |
| Miconic | 150 | 55 | +6 | -1 | 0 | -5 | 58.3 | 8.7 | 3.4 | 1 |
| NoMystery | 20 | 8 | +10 | +1 | +1 | 0 | 2497 | 128 | 29.1 | 1.1 |
| OpenStack11 | 20 | 17 | +2 | +2 | +1 | 0 | 2.1 | 2 | 1.8 | 2 |
| ParcPrint11 | 20 | 6 | +5 | +3 | +1 | +14 | 869 | 10 | 1.5 | 21826 |
| Rovers | 40 | 6 | +2 | +1 | 0 | +1 | 33.4 | 9.6 | 1.7 | 2 |
| Satellite | 36 | 6 | 0 | 0 | 0 | 0 | 72.9 | 35.3 | 9.9 | 10.7 |
| TPP | 30 | 6 | 0 | 0 | 0 | 0 | 6.5 | 3.4 | 1 | 1 |
| Trucks | 30 | 6 | +2 | 0 | 0 | 0 | 24.8 | 21.9 | 2.8 | 1 |
| VisitAll11 | 20 | 9 | 0 | 0 | 0 | 0 | 30 | 25.5 | 1 | 1 |
| Woodwork11 | 20 | 3 | +9 | +5 | +4 | +6 | 1059 | 116 | 92.2 | 514 |
| Zenotravel | 20 | 8 | +1 | 0 | 0 | 0 | 41.6 | 1.5 | 1.1 | 1 |
| $\Sigma$ | 1271 | 605 | +57 | +16 | +16 | +8 |  |  |  |  |

## Experimental Results: LM-cut

|  | Coverage |  |  |  |  | Evaluations |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Domain | \# | A | L | S | B | P | L | S | B | P |
| Airport | 50 | 28 | -1 | -1 | -1 | $\mathbf{+ 1}$ | 1 | 1 | 1 | 4.7 |
| Driverlog | 20 | 13 | 0 | 0 | 0 | 0 | 1.9 | 1.2 | 1.2 | 1 |
| Floortile11 | 20 | 7 | $\mathbf{+ 1}$ | $\mathbf{+ 1}$ | 0 | 0 | 6.4 | 6.4 | 1 | 1 |
| Gripper | 20 | 7 | $\mathbf{+ 7}$ | $\mathbf{+ 7}$ | $\mathbf{+ 7}$ | 0 | 14662 | 14662 | 10049 | 1 |
| Logistics00 | 28 | 20 | 0 | 0 | 0 | 0 | 1.9 | 1.1 | 1.1 | 2.9 |
| Miconic | 150 | 141 | 0 | 0 | 0 | 0 | 2.1 | 1.5 | 1.1 | 1 |
| NoMystery | 20 | 14 | $\mathbf{+ 6}$ | $\mathbf{+ 3}$ | 0 | 0 | 6.5 | 3.1 | 1 | 1 |
| OpenStack11 | 20 | 16 | 0 | 0 | 0 | 0 | 2.5 | 2.4 | 2.1 | 1.8 |
| ParcPrint11 | 20 | 13 | 0 | 0 | 0 | $\mathbf{+ 7}$ | 5 | 1.2 | 1.1 | 1246 |
| Rovers | 40 | 7 | $\mathbf{+ 2}$ | $\mathbf{+ 1}$ | $\mathbf{+ 1}$ | $\mathbf{+ 2}$ | 6.1 | 3.8 | 1.2 | 4.4 |
| Satellite | 36 | 7 | $\mathbf{+ 3}$ | $\mathbf{+ 3}$ | $\mathbf{+ 3}$ | $\mathbf{+ 4}$ | 4.8 | 1.8 | 1.7 | 21.5 |
| TPP | 30 | 6 | $\mathbf{+ 1}$ | $\mathbf{+ 1}$ | $\mathbf{+ 1}$ | 0 | 1.2 | 1.1 | 1 | 1 |
| Trucks | 30 | 10 | 0 | 0 | 0 | 0 | 2.7 | 2.3 | 1 | 1 |
| VisitAll11 | 20 | 10 | $\mathbf{+ 1}$ | $\mathbf{+ 1}$ | 0 | 0 | 7 | 6.8 | 1 | 1 |
| Woodwork11 | 20 | 12 | $\mathbf{+ 5}$ | $\mathbf{+ 4}$ | $\mathbf{+ 4}$ | $\mathbf{+ 7}$ | 91.6 | 23.8 | 17 | 772 |
| Zenotravel | 20 | 13 | 0 | 0 | 0 | 0 | 3.6 | 1.6 | 1 | 1 |
| $\sum$ | 1271 | 833 | $\mathbf{+ 2 0}$ | $\mathbf{+ 1 4}$ | $\mathbf{+ 1 7}$ | $\mathbf{+ 3 8}$ |  |  |  |  |

## Experimental Results: Search Time



## Experimental Results: Total Time



Max partition size: 100000 transitions


Max partition size:
10000 transitions

## Conclusions

- Novel method of dominance pruning useful for many domains
- Overhead in computing the relation and comparing states during the search
- Future work:
- Find coarser relations
- Reduce overhead
- Irrelevance pruning
$\rightarrow$ SoCS talk on Thursday (joint session with ICAPS)!


## Thank you for your attention!

## Questions?

