#### Model Checking, Performance Evaluation, Synthesis and Optimization of Cyber-Physical Systems



# Kim G. Larsen



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#### Model Checking, Performance Evaluation, Synthesis and Optimization of Cyber-Physical Systems



# Kim G. Larsen



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#### Overview

- Timed Automata / UPPAAL
  - Verification
- Stochastic Priced Timed Automata / UPPAAL SMC
  - Performance Evaluation
  - SMC in a Nutshell
  - Stochastic Hybrid Automata
- Timed Games / UPPAAL TIGA
  - Controller Syntesis

Train Crossing Brick Sorting,Production Cell, HYDAC Case

Stochastic Priced Timed Games / UPPAAL STRATEGO

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- Optimal & Safe Synteses
- Conclusion

Train Crossing Schedulability Analysis Wireless Sensor Networks Energy Aware Building

Train Crossing Go-To-Work Adaptive Cruice Control Floor Heating

**Train Crossing** 



# Timed Games







#### **Timed Automata & Model Checking**



State (L1, x=0.81) Transitions (L1, x=0.81) -2.1 ->(L1, x=2.91) ->(goal, x=2.91)

E⟨⟩ goal ? A⟨⟩ goal ? A[] ¬ L4 ?

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#### **Timed Games & Synthesis**



Question Does their exist a strategy that guarantees A<> Goal ?

**Strategy**:  $\sigma: (\ell, v) \mapsto \{\lambda, c_{act}\}$ 

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### **Decidability of Timed Games**

#### Theorem [AMPS98, HK99]

Reachability and safety timed games are decidable and EXPTIME-complete. Furthermore memoryless and "region-based" strategies are sufficient.

 $\sim$  classical regions are sufficient for solving such problems

#### Theorem [AM99,BHPR07,JT07]

Optimal-time reachability timed games are decidable and EXPTIME-complete.

[AM99] Asarin, Maler. As soon as possible: time optimal control for timed automata (HSCC'99).
 [BHPR07] Brihaye, Henzinger, Prabhu, Raskin. Minimum-time reachability in timed games (ICALP'07).
 [JT07] Jurdziński, Trivedi. Reachability-time games on timed automata (ICALP'07).

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#### **Computing Winning States**





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### **Reachability Games**

**Backwards Fixed-Point Computation** 

Х

Y

 $Pred_t(X,Y)$ 

#### Definitions

 $\pi(X) = \text{Pred}_{t}[X \cup c\text{Pred}(X), u\text{Pred}(X^{C})]$ 

#### Theorem:

The set of winning states is obtained as the least fixpoint of the function:  $X \mapsto \pi(X) \cup Goal$ 

#### Symbolic On-the-fly Algorithms for Timed Games [CDF+05, BCD+07]

-S.S'	Initialization:
-G	$Passed \leftarrow \{S_0\}$ where $S_0 = \{(\ell_0, \vec{0})\}^{\nearrow}$ ;
is the set of (concrete) goal states;	Waiting $\leftarrow \{(S_0, \alpha, S') \mid S' = Post_{\alpha}(S_0)^{\nearrow}\};\$
$-E = \{S \xrightarrow{\sim} S', S \xrightarrow{\sim} S'\}$ the (finite) set of symbolic transitions (controlle	$Win[S_0] \leftarrow S_0 \cap (\{Goal\} \times \mathbb{R}^X_{\geq 0});$
$-Waiting \subseteq E$	$Depend[S_0] \leftarrow \emptyset$ :
is the list of symbolic transitions waiting to be p	$= \circ_F \circ \cdots \circ [\circ \circ] = \circ$
- Passed	Main:
is the list of the passed symbolic states; $-Win[S] \subseteq S$	while $((Waiting \neq \emptyset) \land (s_0 \notin Win[S_0]))$ do
is the subset of $S$ currently known to be winning	$e = (S, \alpha, S') \leftarrow pop(Waiting);$
$- Depend[S] \subseteq E$	if $S' \notin Passed$ then
indicates the edges (predecessors) of S which mu information about S is obtained	$Passed \leftarrow Passed \cup \{S'\};$
	$Depend[S'] \leftarrow \{(S, \alpha, S')\};$
	$Win[S'] \leftarrow S' \cap (\{Goal\} \times \mathbb{R}^X_{\geq 0});$
	$Waiting \leftarrow Waiting \cup \{(S', \alpha, S'') \mid S'' = Post_{\alpha}(S')^{\nearrow}\};$
	if $Win[S'] \neq \emptyset$ then $Waiting \leftarrow Waiting \cup \{e\}$ :
	$(* reevaluate *)^a$
symbolic version of on-the-fly MC alg	gorithm $Win^* \leftarrow \operatorname{Pred}_t(Win[S] \cup [ ] \subset \operatorname{Pred}_c(Win[T]))$
for modal mu-calculus	$\bigcup_{S \to T} \operatorname{Pred}_{\mathcal{C}}(T \setminus Win[T])) \cap S$
Liu & Smolka 98	$\bigcup_{S \xrightarrow{u} T} \operatorname{Ied}_u(I \setminus \operatorname{Vin}[I])) \mapsto S,$
	If $(Win[S] \subsetneq Win^+)$ then
	$Waiting \leftarrow Waiting \cup Depend[S]; Win[S] \leftarrow Win^*;$
	$Depend[S'] \leftarrow Depend[S'] \cup \{e\};$
	endif
	endwhile

[CDF+05] Cassez, David, Fleury, Larsen, Lime. Efficient on-the-fly algorithms for the analysis of timed games (CONCUR'05). [BCD+07] Berhmann, Cougnard, David, Fleury, Larsen, Lime. Uppaal-Tiga: Time for playing games! (CAV'07).

#### Model Checking (ex Train Gate)



#### Synthesis (ex Train Gate)





# DEMO





#### A Buggy Brick Sorting Program



## **Brick Sorting**



# DEMO





#### **Brick Sorting**



## **Production Cell Overview**

- Realistic casestudy described in several formalisms (1994 and later).
- Objective: stamp metal plates in press.
- feed belt, two-armed robot, press, and deposit belt.



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### Production Cell in UPPAAL Tiga



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### **Experimental Results**

#### [CDF+05]

Pla	Plates Basic		Basic +inc		Basic +inc		Basic + lose + inc		Basic+lose +inc		
					+pruning		+pruning		+topt		
		time	mem	time	mem	time	mem	time	mem	time	mem
2	win	0.0s	1M	0.0s	1M	0.0s	1M	0.0s	1M	0.04s	1M
2	lose	0.0s	1M	0.0s	1M	0.0s	1M	0.0s	1M	n/a	n/a
R	win	0.5s	19M	0.0s	1M	0.0s	1M	0.1s	1M	0.27s	4M
5	lose	1.1s	45M	0.1s	1M	0.0s	1M	0.2s	3M	n/a	n/a
Δ	win	33.9s	1395M	0.2s	8M	0.1s	6M	0.4s	5M	1.88s	13M
4	lose	-	-	0.5s	11M	0.4s	10M	0.9s	9M	n/a	n/a
5	win	-	-	3.0s	31M	1.5s	22M	2.0s	16M	13.35s	59M
5	lose	-	-	11.1s	61M	5.9s	46M	7.0s	41M	n/a	n/a
6	win	-	-	89.1s	179M	38.9s	121M	12.0s	63M	220.3s	369M
0	lose	-	-	699s	480M	317s	346M	135.1s	273M	n/a	n/a
7	win	-	-	3256s	1183M	1181s	786M	124s	319M	6188s	2457M
1	lose	-	-	-	-	16791s	2981M	4075s	2090M	n/a	n/a

Model	С	3	<b>c</b> 6		c12		u3		u6		u12	
Old	0.1s	1M	12s	63M	-	-	0.2s	3M	235s	273M	-	-
New	0.05s	3.5M	0.05s	3.5M	0.14s	55M	0.02s	3.5M	0.04s	3.5M	0.12s	55M

[BCD+07]

[CDF+05] Cassez, David, Fleury, Larsen, Lime. Efficient on-the-fly algorithms for the analysis of timed games (CONCUR'05). [BCD+07] Berhmann, Cougnard, David, Fleury, Larsen, Lime. Uppaal-Tiga: Time for playing games! (CAV'07).

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#### Plastic Injection Molding Machine



[CJL+09]



- Robust and optimal control
- Tool Chain
  - Synthesis: UPPAAL TIGA
  - Verification: **PHAVer**
  - Performance: SIMULINK
- 40% improvement of existing solutions..

[CJL+09] Cassez, Jessen, Larsen, Raskin, Reynier. Automatic Synthesis of Robust and Optimal Controllers – An Industrial Case Study (HSCC'09).

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## **Oil Pump Control Problem**





 R1: stay within safe interval [4.9,25.1]

 R2: minimize average/overall oil volume

$$\int_{t=0}^{t=T} v(t) dt / T$$

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## The Machine (consumption)



- Infinite cyclic demand to be satisfied by our control strategy.
- P: latency 2 s between state change of pump

F: noise 0.1 l/s



Juasiomodo

#### **Hybrid Game Model**



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### **Abstract Game Model**



- UPPAAL Tiga offers games of perfect information
- Abstract game model such that states only contain information about:
  - Volume of oil at the beginning of cycle
  - The ideal volume as predicted by the consumption cycle
  - Current time within the cycle
  - State of the Pump (on/off)
  - Discrete model

D					
V, V_rate					
V_acc					
time					

## Machine (uncontrollable)





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### Pump (controllable)



Quasiomodo

## **Global Approach**



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## **Tool Chain**







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# Stochastic Priced Timed Games





## Going to Sydney – in 1 hour



Can I get to Sidney? (1-player)

Will I always come to Sidney? (1-player)

What is the optimal WC strategy? (2-player)

Is there a strategy guaranteeing  $WC \le 60$ ? (2-player)

What is the optimal strategy? (1½-player)

What is the optimal strategy Guarenteeing WC  $\leq 60$ ? (1½-player)

lakob H.

Taankvist [33]

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## **Timed Games**





Strategy:

 $\sigma: Exec_{\mathcal{G}}^{f} \rightharpoonup \mathcal{P}\left(\Sigma_{c} \cup \{\lambda\}\right) \setminus \{\emptyset\}$ 

 Memoryless, deterministic, most permissive.

#### Run

$$\pi = (\text{INIT}, x = 0) \xrightarrow{50.1 \text{ r}} (\text{CHOICE}, x = 0) \xrightarrow{2.4 \text{ a}} (A, x = 0) \xrightarrow{20.3 \text{ d}} (\text{END}, x = 20.3)$$

Total time = 50.1 + 2.4 + 20.3 = 72.8

ATVA 2014, November 4, 2014

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#### Timed Games –

#### **Time Bounded Reachability**

**Objective**:  $A\langle\rangle$  (END  $\land$  time  $\leq 210$ )



### **Priced** Timed Games





take b immediately
 WC= 280



### Priced Timed MDP





- Cost optimal strategy

   take b immediately
   WC= 280
- Priced Timed MDP
- Optimal expected cost str
  - take b immediately expectation = 160



### Priced Timed MDP





- Cost optimal strategy
  - take b immediately overall = 280
- Priced Timed MDP
- Optimal expected cost str
  - take b immediately expectation = 160
- Minimal Expected Cost while guaranteeing END is reached within time 210:

Strat.: t>90→ (100,w)

- t>70→ (0,a)
- t<70→ (0,b)

= 204

#### **Stochastic Strategies** for Learning!



### **Reinforcement Learning**



#### **Strategies - Representation**



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**Covariance Matrices** 



a b

ATVA 2014, November 4, 2014

Kim Larsen [42]

#### **Covariance Matrices**



λ a b

ATVA 2014, November 4, 2014

#### Kim Larsen [43]

**Covariance Matrices** 



ATVA 2014, November 4, 2014

Kim Larsen [44]

#### **Covariance Matrices**



λ a b

ATVA 2014, November 4, 2014

#### **Covariance Matrices**



ATVA 2014, November 4, 2014

**Covariance Matrices** 



a b

λ

ATVA 2014, November 4, 2014

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## Going to Sydney – in 1 hour



Can I get to Sidney? (1-player)

Will I always come to Sidney? (1-player)

What is the optimal WC strategy? (2-player)

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What is the optimal strategy? (1½-player)

What is the optimal strategy Guarenteeing WC  $\leq 60$ ? (1½-player)

lakob H.

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# DEMO





### Safe and Optimal Train Gate



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# DEMO





### Safe & Adaptive Cruice Control



Q1: Find a safety strategy for *Ego* such no crash will ever occur no matter what *Front* is doing.
Q2: Find the most permissive strategy ensuring safety
Q3: Find the optimal sub-strategy that will allow *Ego* to go as far as possible (without overtaking).

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#### Discretization



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#### Continuous





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#### **No Strategy**



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### Safety Strategy



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#### Safety Strategy

inf{velosityFront-velosityEgo==v}: distance under safe



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### **Optimal and Safe Strategy**

strategy safeFast = minE (D) [<=100]: <> time >= 100 under safe



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#### **Other Case Studies**



### Floorheating









Thursday Afternoon Daniel Lux, Seluxit Marco Muniz, AAU

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Learning, Analysis, SynthesiS and Optimization of Cyber-Physical Systems





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# **Applications**





### **Case Studies: Controllers**

- Memory Arbiter Synthesis and Verification for a Radar Memory Interface Card, 2005
- Analyzing a χ model of a turntable system using Spin, CADP and Uppaal, 2006
- Designing, Modelling and Verifying a Container Terminal System Using UPPAAL, 2008
- Model-based system analysis using Chi and Uppaal: An industrial case study, 2008
- Climate Controller for Pig Stables, 2008 (synth)

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 Optimal and Robust Controller for Hydralic Pump, 2009 (synth)

## References

- Frits Vaandrager: <u>A first introduction to UPPAAL</u>
- Alexandre David, <u>Kim G Larsen: More features in UPPAAL</u>
- Alexandre David, Kim G Larsen, Axel Legay, Marius Mikucionis, Danny Bøgsted Poulsen: <u>UPPAAL SMC Tutorial</u>. To appear in Software Tools for Technology Transfer.
- Alexandre David, Kim G. Larsen, Axel Legay, Marius Mikucionis, Zheng Wang: <u>Time for Statistical Model Checking</u> of Real-Time Systems. CAV 2011.
- Gerd Behrmann, Agnes Cougnard, Alexandre David, Emmanuel Fleury, Kim G. Larsen, and Didier Lime: <u>UPPAAL-Tiga: Time for</u> <u>Playing Games!</u> CAV 2007.
- Alexandre David, Peter Gjøl Jensen, Kim Guldstrand Larsen, Marius Mikucionis, Jakob Haahr Taankvist: <u>Uppaal Stratego</u>. TACAS 2015
- For more see

http://people.cs.aau.dk/~kgl/SSFT2015/

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#### **Case Studies: Protocols**

- Analysis of a protocol for dynamic configuration of IPv4 link local addresses using Uppaal, 2006
- Formalizing SHIM6, a Proposed Internet Standard in UPPAAL, 2007
- Verifying the distributed real-time network protocol RTnet using Uppaal, 2007
- Analysis of the Zeroconf protocol using UPPAAL, 2009
- Analysis of a Clock Synchronization Protocol for Wireless Sensor Networks, 2009

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 Model Checking the FlexRay Physical Layer Protocol, 2010

### Using UPPAAL as Back-end

- Timed automata translator from Uppaal to PVS
- Component-Based Design and Analysis of Embedded Systems with UPPAAL PORT, 2008
- METAMOC: Modular WCET Analysis Using UPPAAL, 2010.

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 TetaSARTS: a tool for modular timing analysis of safety critical Java systems, 2013

#### www.uppaal.org

#### UPPAAL

#### Home

Home | About | Documentation | Download | Examples | Bugs

UPPAAL is an integrated tool environment for modeling, validation and verification of real-time systems modeled as networks of timed automata, extended with data types (bounded integers, arrays, etc.).

The tool is developed in collaboration between the <u>Department of Information Technology</u> at Uppsala University, Sweden and the <u>Department of Computer</u> <u>Science</u> at Aalborg University in Denmark.



#### Download

Figure 1: UPPAAL on screen.

The current official release is UPPAAL 3.4.11 (Jun 23, 2005). A release of UPPAAL **3.6 alpha 3** (dec 20, 2005) is also available. For more information about UPPAAL version 3.4, we refer to this <u>press release</u>.







#### RELATED SITES: TIMES | UPPAAL CORA | UPPAAL TRON

#### License

The UPPAAL tool is **free** for non-profit applications. For information about commercial licenses, please email sales(at)uppaal(dot)com.

To find out more about UPPAAL, read this short <u>introduction</u>. Further information may be found at this web site in the pages <u>About</u>, <u>Documentation</u>, <u>Download</u>, and <u>Examples</u>.

#### **Mailing Lists**

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UPPAAL has an open <u>discussion forum</u> group at Yahoo!Groups intended for users of the tool. To join or post to the forum, please refer to the information at the <u>discussion forum</u> page. Bugs should be reported using the <u>bug tracking</u> <u>system</u>. To email the development team directly, please use uppaal(at)list(dot)it(dot)uu(dot)se.

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