Abstract. Modern traffic lights use information from induction loops and to some extend radar information. Recent developments in radar technology has made it possible to obtain more detailed information relevant to the control mechanism of the traffic light. Unfortunately much of the current controllers do not profit from this additional information. Using this information could minimize waiting times and energy waste.

Uppaal Stratego is a tool that combines machine learning and model checking techniques to synthesize near optimal control strategies. The tool has been applied successfully to several case studies e.g. battery optimization in satellites, safe and optimal cruise control and optimal floor heating controlling.

In this work we use Uppaal Stratego as an on-line controller for a signalised intersection. Our controller reads the current data from the radar sensors and effectively uses it to learn a near optimal controller at each control step. Our experiments report considerable reduction in the waiting times.

Keywords: traffic lights, model checking, machine learning, optimization.

1 Introduction

Traditionally, traffic signal control strategies are based on loop detectors embedded in the road surface. The loop detectors give a precise location of vehicles passing or occupying the loops, but the prediction of the vehicle dynamics is limited by the detector locations.

The corresponding control strategies are discrete event-based with incremental extensions of green times supplemented with a number of specific decision rules. Despite the development of new computer based signal controllers there has been little development in the field of control strategies. With the most recent development in radar detection systems, radar detectors are feasible for road traffic detection. One radar detector, placed appropriately, can replace all the detector loops in one intersection approach. It can monitor the approach continuously and give a full account of all vehicles approaching the junction. This would allow for a continuous modelling of traffic into the junction and for a control approach based on realistic vehicle arrival prediction.

The Danish Congestion Commission calls in its recent report [8] for improved traffic signal control in order to reduce congestion, travel time and energy consumption. This project has been formulated to contribute to a more efficient utilisation of the existing infrastructure by improving traffic signal control.

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**Aim** The aim of this paper is to improve traffic management and control in order to reduce congestion, energy consumption and CO₂ emissions. In this paper specifically to develop an efficient traffic signal control strategy that takes advantage of the continuous traffic monitoring made available by radar detectors. The purpose of the strategy is to optimize the total traffic flow in the junction, i.e. to reduce the total delay and queue length.

In fact, the method and tool we use for synthesizing control strategies allows for making trade-off between these various optimization criteria.

## 2 Preliminaries

### 2.1 Uppaal Stratego

Uppaal Stratego [2,3] is a branch of the Uppaal [1] family of software tools. Uppaal Stratego can be used to learn strategies for complex systems, in this case controlling the lights in a crossing. In Fig. 1 we see an example of a Uppaal Stratego model, a Timed Game Automata.

We model a car approaching a town, the driver can choose to go around the town or through it. In the town there is a signal controlled crossing. If the driver is lucky the light will be green, and if he is unlucky the light will be red.

In the model the circles denote states and the arrows denote transitions between the states. In the first state **Start** the driver can choose whether to go through the town or around it. As the driver makes this choice the transitions are solid arrows. If he chooses to go around the town the time it will take will be chosen from a uniform distribution between 20 and 25, the driver cannot affect this, thus the transitions are dashed. If the driver chooses to go through the town there is \( p \) chance that the lights are green and \( 1 - p \) chance they will be red. We then see in the model that the time to reach **Goal** are again chosen from uniform distributions; 5 to 10 for **Green** and 15 to 60 for **Red**.

Clearly the drivers choice depends on the value of \( p \), we will consider \( p_1 = \frac{3}{4} \) and \( p_2 = \frac{1}{4} \). If we let the driver choose uniformly random we can use Uppaal Stratego to estimate the expected time to reach **Goal**. For \( p_1 \) this is 18.8 and for \( p_2 \) it is 26.3. However the driver should not choose randomly, we therefore use Uppaal Stratego to learn a strategy which minimizes the time to reach **Goal**. For the scenario with \( p_1 \) Uppaal Stratego learns to go through the town as the probability of green is high, this leads to an expected time to **Goal** of 15.0. On the other hand if we have \( p_2 \) Uppaal Stratego learns to go around the town leading to an expected time to **Goal** of 22.5.

![Fig. 1: Example of Uppaal Stratego model, a Timed Game Automata, modeling a car passing a town.](image)

The example in Fig. 1 is quite simple, and it is easy to compute the optimal strategy manually. However with more states and more decisions to be made it quickly becomes impossible
manually to compute a strategy. It is then possible to use 

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Uppaal Stratego has already been used for several case studies. In one case study it was used to learn a controller for adaptive cruise control [7]. In the case study there were two cars, the front car controlled by the environment and the ego car controlled by the controller. We here used another feature of Uppaal Stratego to find the set of actions which were safe in the sense that it would be impossible to hit the other car no matter how the other car drove. After doing that we learned a strategy which made ego stay as close as possible to the front car, but without ever crashing into it.

In another case study Uppaal Stratego was used to learn strategies for controlling the floor heating in a real house [6]. Several techniques were developed to be able to deal with the complexity of a real house. The project resulted in an up to almost 60% improvement in the distance from the target temperatures. For this case study a full tool chain all the way from Uppaal Stratego to the relays in the house has been build, enabling Uppaal Stratego to control the physical floor heating system in the house.

2.2 Simulation of Urban MOBility - SUMO

SUMO [4] is an open source tool which allows to model and simulate traffic systems. It provides a number of supporting tools which allow for visualization, network transformation, waiting time calculations, traffic light performance, etc. SUMO provides features for modelling a vast number of scenarios and possibilities to inter-operate with other tools. There is also a wide active community which offer support.

In this work we mainly use the following SUMO components. Road networks which allow to model the relevant part of the map, roads lanes and intersections. Vehicles which allow to realisticaly model the traffic demand [5]. Traffic lights which allow to model a signalized intersection. Induction loops which indicate if a car is on the given detector. Area detectors which indicate the number of cars moving or jammed in an area. Area detectors allow us to simulate radars. Traci a software interface that gives access to objects in the running simulation. We use induction loop and area detector information to improve the control of a given traffic light. Netconvert which allows to import maps from open street maps. In Section 4, we will use SUMO and the above features to model a real crossing from the Køge municipality in Denmark.

3 Case Study

3.1 Description of the intersection

Figure 2 shows the intersection with the two directions A and B. In direction A there is a separate left turn lane and a combined lane for right turn and the straight ahead direction. In direction B there is at combined lane for all three directions. Figure 2 also shows where the loops are placed and the radar area. In direction A crossing loops are placed at distances, 70 and 120 meters from the stop line (a crossing loop is a loop which detects when a car hits the line which the loops cover). In direction B there is a crossing loop 70 meters from the stop line and a 15 meter long presence loop behind the stop line. (a presence loop is a loop that detects when there are cars in the area the loop covers)

3.2 Traffic

To make the simulation as simple as possible, we will only consider passenger cars. Figure 3 shows the MAX traffic in a one hour (peak hour) scenario. We also have two more scenarios: MID traffic = 60% of traffic in max traffic and LOW traffic = 30% of traffic in max traffic. The figures in the Max traffic scenarios are close to the capacity of the intersection and gives with
Fig. 2: Intersection between Nylandsvej and Værkstedvej at Køge municipality. Layout of loops and radar area.

Fig. 3: Peak hour “MAX” traffic per direction.
the time based controller large delay time and queues. In the simulation the cars’ mean speed is chosen to be 50 \text{ km/h}. In the rest of the paper, we will use MAX, MID, and LOW to refer to the max, middle and low traffic scenarios.

3.3 Controlling Strategies for Operation of the Signalized Intersection

The intersection signal has two phases. The signal has an interval with yellow of 8 seconds when switching between the two phases. A green phase has a minimal duration of 8 seconds. We consider two controllers in the intersection. A static time controller and an induction loop based controller.

Static Time Controller The static time controller cycles with a fixed duration among the two phases. The durations vary according to the traffic load. The phase durations for the different traffic load scenarios are given in Table 1. In the rest of the paper we will use Static to refer to this controller.

Loop Controller The loop controller uses the induction loops and presence detectors as shown in Figure 2 for better control. The controller operates as follows:

1. The signal must always return to green in direction A if there is no notification from direction B. (The signal has resting position in green in direction A.)
2. The crossing loops extend the actual green time with 4.0 seconds when they are passed until the max extension time in Table 1 is reached.
3. The presence loop in direction B extend the green time for direction B until the max extension time from Table 1 is reached.
4. If there is a notification from direction B the crossing loops in direction A will extend the green phase in direction A with 4.0 seconds until a max green time from Table 1 is reached.

In the rest of the paper we will refer to this controller as the Loop controller.

4 Modeling, Optimization and Simulation

In order to analyze and improve the traffic flow for the scenario described in Section 3, we need a faithful model. In this section, we first describe the SUMO road network model for the intersection. Then we describe how to model the traffic demand described in Section 3.2. Finally we describe the model of the traffic light, the controllers described in Section 3.3 and our UpPAAL STRATEGO controller.

4.1 Network Model

Figure 4 illustrates the SUMO road networks for the intersection, the networks are obtained from Open Street maps with some adjustments. Figure 4 left shows the SUMO loop detectors and area detectors placed at the distances specified in Section 3.1. Figure 4 right shows the SUMO area detectors which we use to simulate radars. In the network, the lane speed is 50 \text{ km/h}.
4.2 Traffic Demand Model

Section 3.2 describes different traffic load scenarios. In our SUMO model we generate the traffic demand with vehicles, routes and probability distributions on the routes.

Vehicles SUMO allows to define a number of vehicle types, every type with different attributes e.g. acceleration, max speed, etc. An attribute sigma indicates the driver’s imperfection [5]. As mentioned in Section 3.2 we only consider passenger cars these have acceleration $0.8 \text{m/s}^2$, deceleration $4.5 \text{m/s}^2$, length $5\text{m}$ and max speed $50\text{km/h}$. Apart from that we define the minimum distance between the cars to be $2.5\text{m}$ and sigma to be $0.5$.

Routes For every leg of the intersection e.g. A1, B2, there are 3 possible directions, this gives a total of 12 possible directions. For every direction we define a SUMO route. In the simulation vehicles are assigned to routes.

Load Figure 2 right shows the max traffic load for all possible directions. For every direction we model the traffic load using the following Poisson distribution:

$$P(k \text{ cars in an hour}) = \frac{\lambda^k \cdot e^{-\lambda}}{k!}$$

Where $\lambda$ is the average number of cars per hour for a given direction. In the case of the MID and LOW load scenarios we multiply $\lambda$ by 60% or 30% respectively. To generate the corresponding SUMO route file, we sample by repeated Bernoulli trials.

4.3 Controller Models

The intersection connects lanes to a total of 12 directions. The traffic light then consists of 12 signals, one for each direction. Different signal configurations are grouped in phases, the signal state of a phase is encoded by a string. There are two main green phases one where A1,A2 are green encoded as “rrrGGgrrrGGg”, and the other one where B1,B2 are green encoded by “GGgrrrGGgrrr”. In the string, “G” represents priority green. We now describe our models for the Static and the Loop given in Section 3.3 as well as our Uppaal Stratego model.

Static Controller The XML below describes the static controller for the MAX load scenario. We have one definition for every scenario MAX, MID and LOW, where the times of the green phases correspond to the ones in Table 1.
Algorithm 1 High level algorithm for the Uppaal Stratego controller

1: Every 5 seconds read areal detector data from SUMO
2: if Traffic Light in green phase then
3:   Use Uppaal Stratego Figure 5 left – to learn whether extend green phase or go to yellow
4: else if Traffic Light in yellow phase then
5:   Run Uppaal Stratego Figure 5 right – to learn which direction should have the next green phase
6: end if

Loop Controller We have implemented the Loop controller from Section 3.3 in SUMO using Traci and Python. The implementation is straightforward from the description. However, it is important to describe how the extension of green times are implemented. To implement the time extension we use a counter count which starts at the minimal green time i.e. 8 seconds and decreases by 1 at every simulation step. If a loop detector is activated we set the value of the counter as follows: count := max(count, 4.0). Note that if we implement the extension as count := count + 4.0, and if 10 cars come in quick succession count will reach values above 30. Using max allows a extension which is just sufficient for cars to reach the next loop or the stop line.

Uppaal Stratego Controller This controller integrates SUMO and Uppaal Stratego using Traci, the controller will read the status of the traffic light and data from the areal detectors every 5 to 8 seconds. Then it will update the Uppaal Stratego model with the new sensor data.

Uppaal Stratego will then learn a strategy for its internal model (not in SUMO) and use that to identify the best phases. The controller will then indicate the next phase for the traffic light. Algorithm 1 describes the overall behavior of the controller. Figure 5 left (right) shows the Uppaal Stratego model for the green (yellow) phases.

The models use a number of features from Uppaal and are rather advanced. We will briefly give a general idea on how the model for the green phase Figure 5 left works. Uppaal will
Table 2: Results of the experiments. We show the mean and the 95 percentile for respectively the waiting time of the cars and the queue length. This is done for each controller in all scenarios.

### 5 Experiments

In this section we compare the performance of the Static, Loop and Uppaal Stratego controllers for the different MAX, MIN and LOW traffic load scenarios. In the MAX scenario from Table 2 we see that the Static is clearly the worst. This is expected as it is build up on assumptions and does not adapt to the actual traffic. In general the Loop has a slightly better performance in direction A, this is likely due to the fact that the Loop is must always return to green in direction A. However in direction B, Stratego is performing significantly better than any of the other controller resulting in a much better overall score, both for the delay and the queue length. This fits with our expectations as the Stratego controller minimizes the overall queue length in the crossing. The MID scenario shows the same general trend as the MAX controller, except that the Static in some cases actually performs better. In the LOW scenario all the controllers performs quite similar, but the Loop controller is in general the best.

In Figure 6 we see boxplots of the waiting times of the cars that passed through the crossing. What we see is that for medium and high traffic the average waiting time for the Stratego controller is lower than for the two others. We also see that in all scenarios the maximum waiting time was the lowest with the Stratego controller. Lastly we see that in the low and medium traffic scenario the Loop has a lower median value than the Stratego controller. This shows

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† Videos of simulations of the controllers can be found on people.cs.aau.dk/ jht/stratego_traffic.php
Fig. 6: Waiting time for the different controllers, in the scenarios MAX, MID and MIN respectively. The solid line represent the median and the dashed line represent the mean.
that fewer cars are waiting, but the cars that are waiting wait longer in the loop controller than in the Stratego controller.

6 Discussion and Further Work

The contributions of this work are twofold. First, we have presented a successful application of machine learning techniques for the synthesis of near optimal traffic light controllers. Second, we have shown that the proper use of the more detailed information from radars can dramatically decrease the waiting times and queue lengths. Our experimental results show that for the MAX scenario the Uppaal Stratego controller can reduce the average waiting times per car from 37 to 13 seconds.

We observe that the Loop controller relies heavily on traffic assumptions, e.g. a 4 second extension for a car to reach the stop line, thus assuming an average speed of 50 km/h. If this assumption does not hold the performance of the Loop controller might decrease. Another assumption for the Loop and the Static controller is that they have fixed maximal green times that depend on the traffic load. Note, that the Uppaal Stratego controller does not rely on these assumptions, and will therefore not be affected by them changing.

Future Work Future works include improving our Stratego controller, to deal with low traffic demand, and to experiments with more heterogeneous scenarios.

Dealing with traffic lights with more phases as well as extending our controller to address green waves.

Currently we evaluate the controllers by using simulations, statistical model checking allows for a more advanced analysis of simulations, and could be used to evaluate the controllers.

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