Decidability and Symbolic Verification

Kim G. Larsen Aalborg University, DENMARK



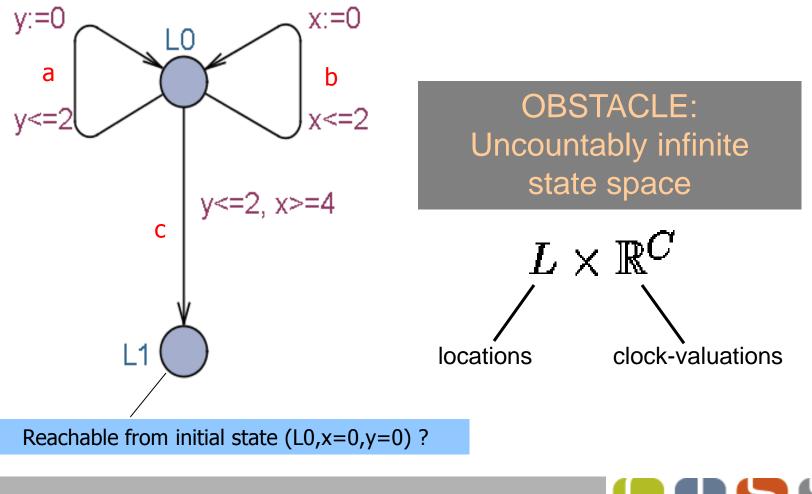


Decidability





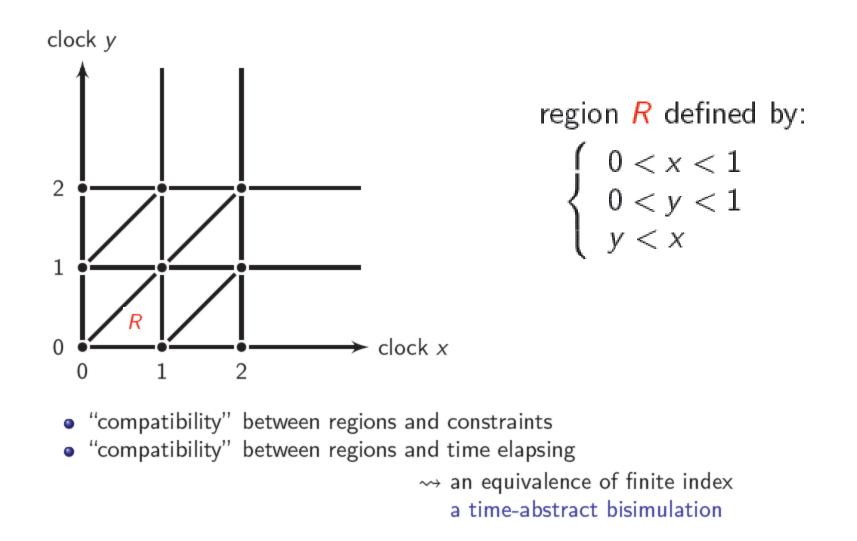
Reachability?



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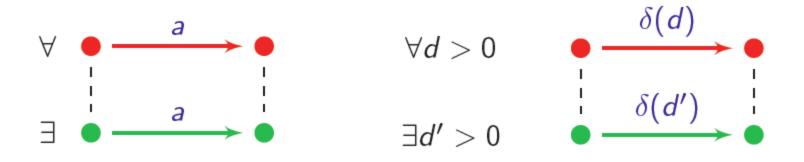
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The Region Abstraction



Time Abstracted Bisimulation

This is a relation between • and • such that:

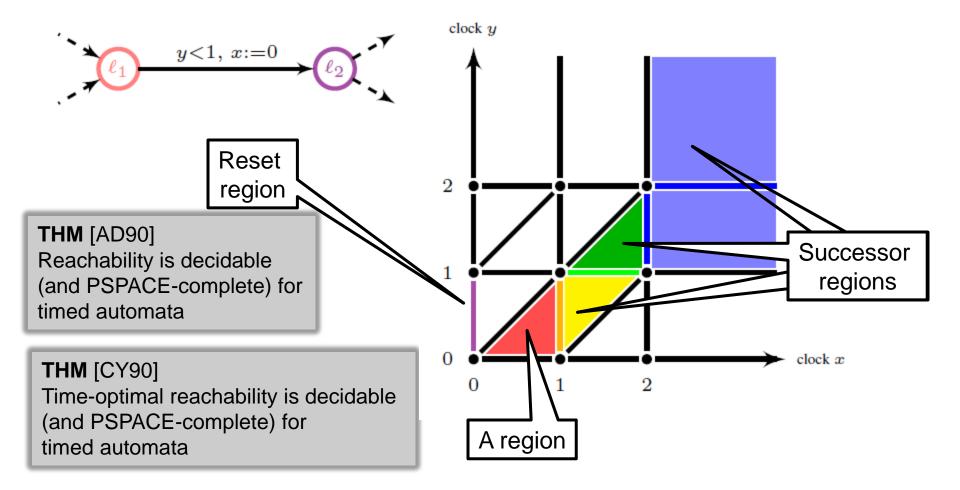


... and vice-versa (swap • and •).





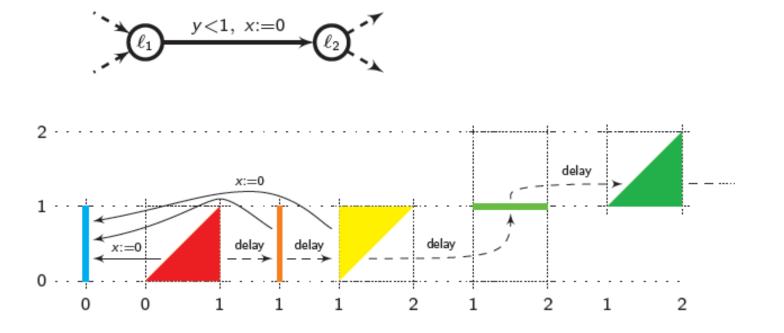
Regions – From Infinite to Finite



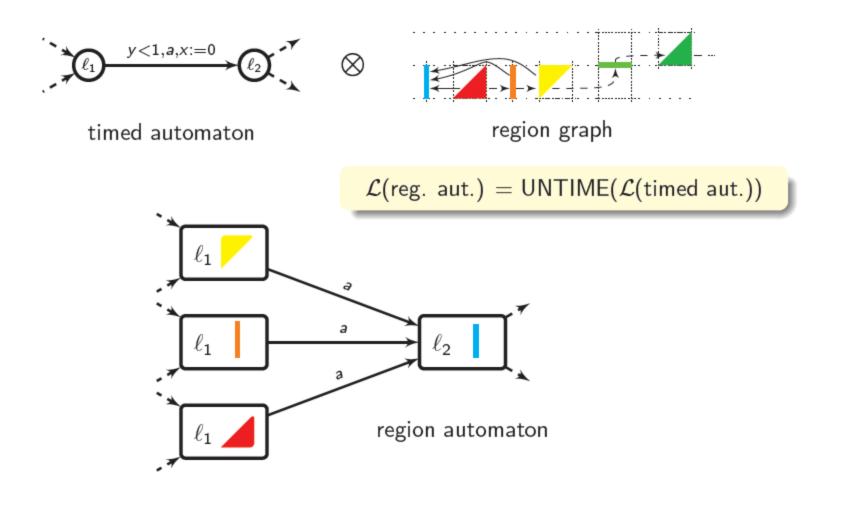
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Region Graph

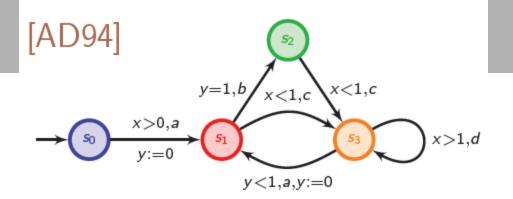
It "mimicks" the behaviours of the clocks.

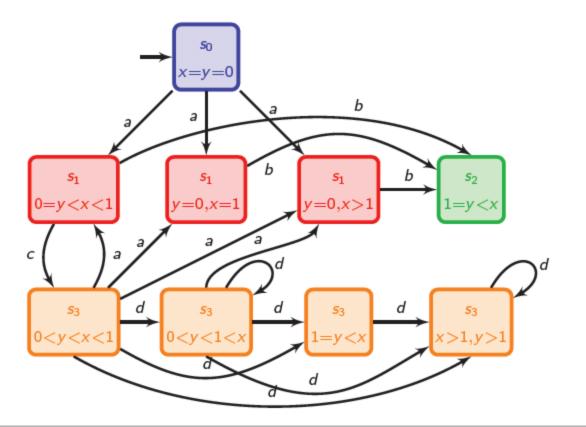


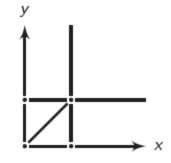
Region Automaton = Finite Bisimulation Quotiont



An Example



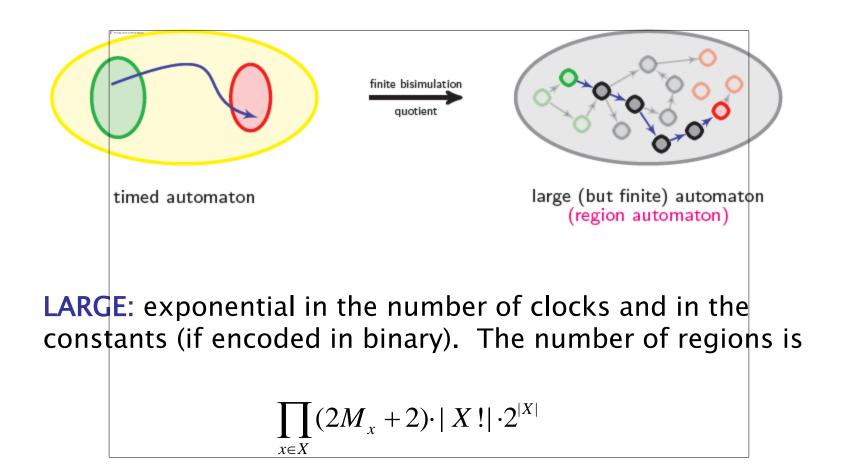




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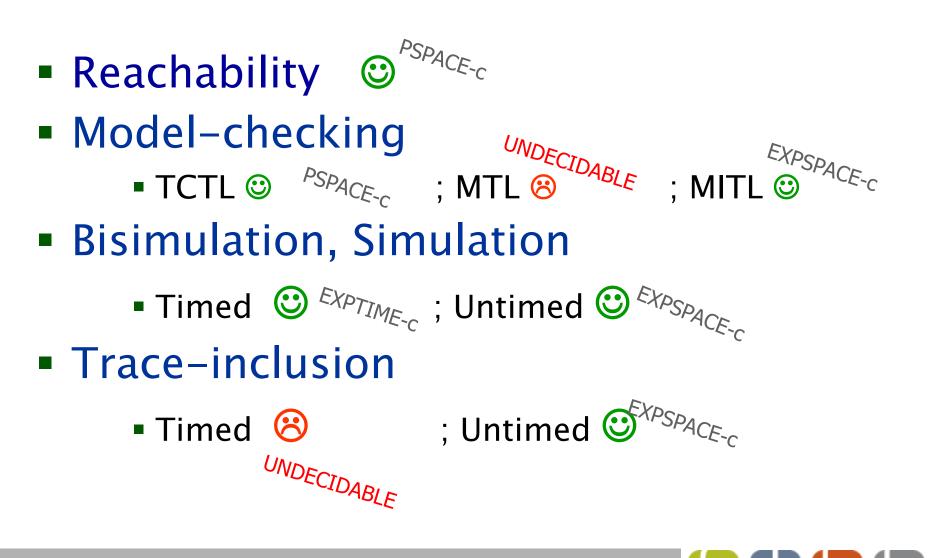
Region Automaton



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Fundamental Results



Kim Larsen [11]

Symbolic Verification

The UPPAAL Verification Engine





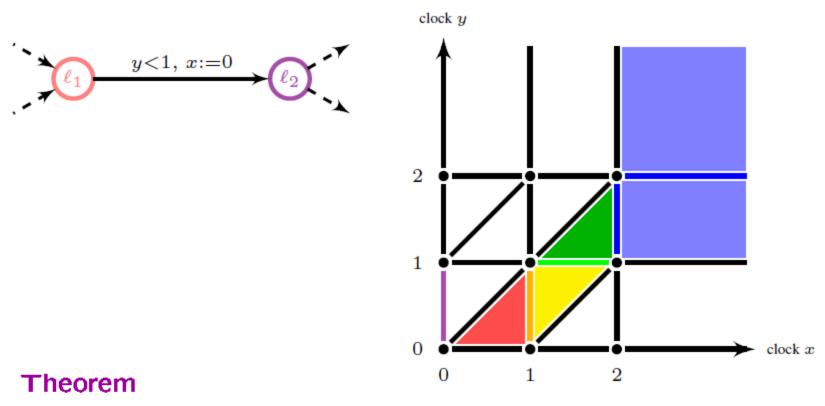
THE "secret" of UPPAAL

😨 C:\Users\kgl\Desktop\DESKTOP12\UPPAAL\UPPAAL examples\LCCC2013\SMC\TrainGateCPS14.xml - UPPAAL
<u>File Edit View Tools Options Help</u>
Editor Simulator ConcreteSimulator Verifier Yggdrasil
Enabled Transitions
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $
…Train(4).x ∈ [23,60]
Viet0 Viet7
Train(5).x ∈ [30,65]
$Train(0) \times -time < -50$
Simulation Trace $Train(0).x - Train(1).x \in [10,20]$
$[Safe, Cross, Stop, Stop, Stop, Stop, Stop, Stop, Occ) = \dots Train(0).x - Train(2).x \in [0,5]$
(Safe, Safe, Stop, Stop, Stop, Stop, Stop, Free) $- \cdots Train(3).x - Train(0).x \in [17,40]$
$no[front()]: Gate \rightarrow Train(5)$
(Safe, Safe, Stop, Sto
$appr[0]: Train(0) \rightarrow Gate[0]$
Trace File: $Train(2).x - Train(1).x \in [7,20]$
Train(3).x - Train(5).x ∈ [-5,0] Train(4).x - time ≤ -33 Cross
-Train(5).x ← Train(0).x ∈ [17,40]
Slow Fast

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Regions – From Infinite to Finite



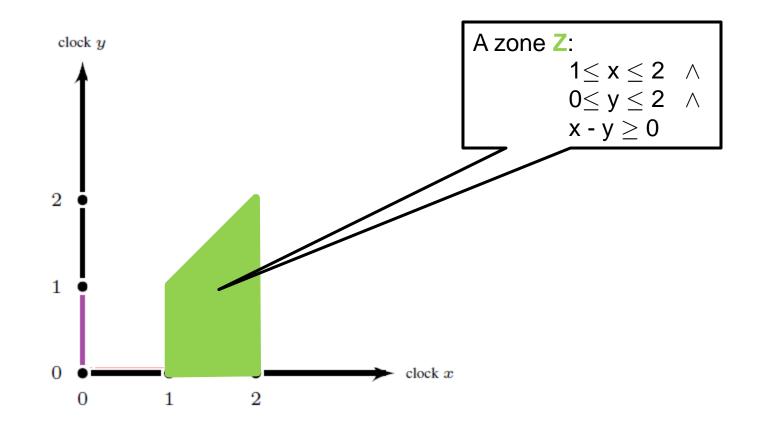
The number of regions is $n! \cdot 2^n \cdot \prod_{x \in C} (2c_x + 2)$.

Region construction: [AD94] In practice: Zones

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Zones – From Finite to Efficiency

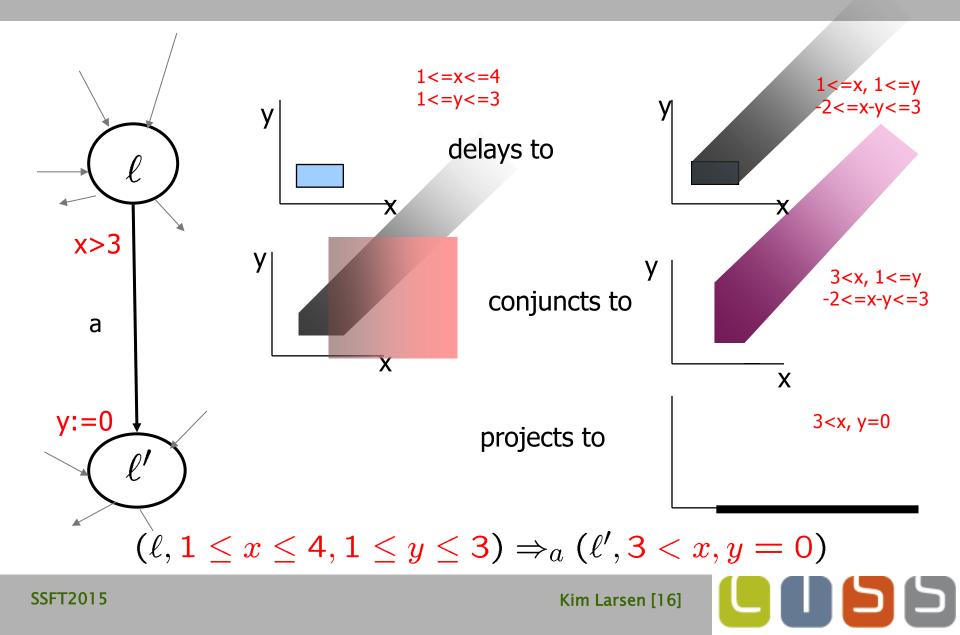


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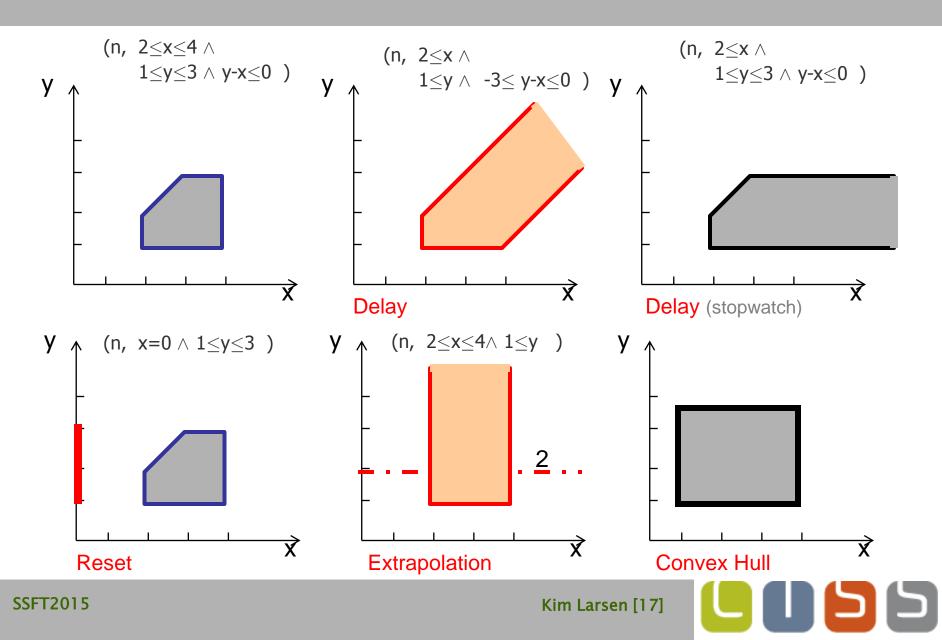
Kim Larsen [15]

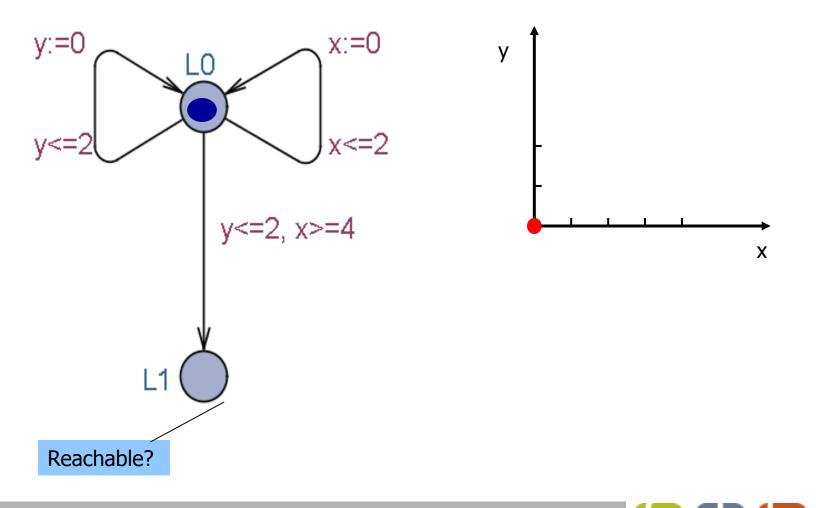


Symbolic Transitions

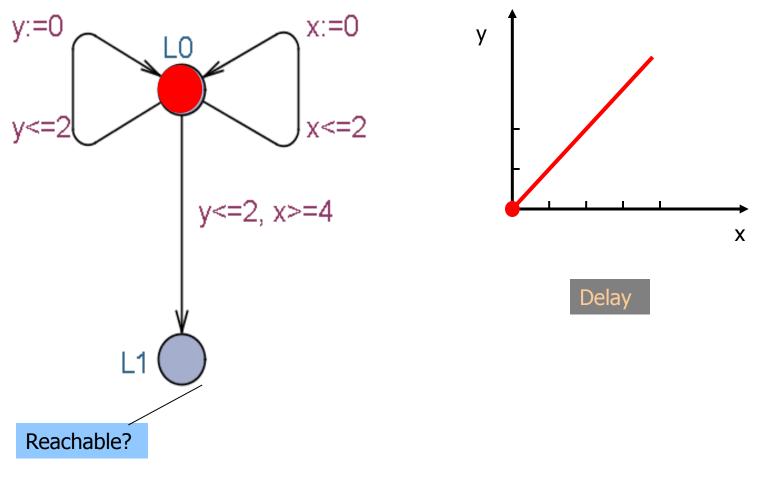


Zones – Operations





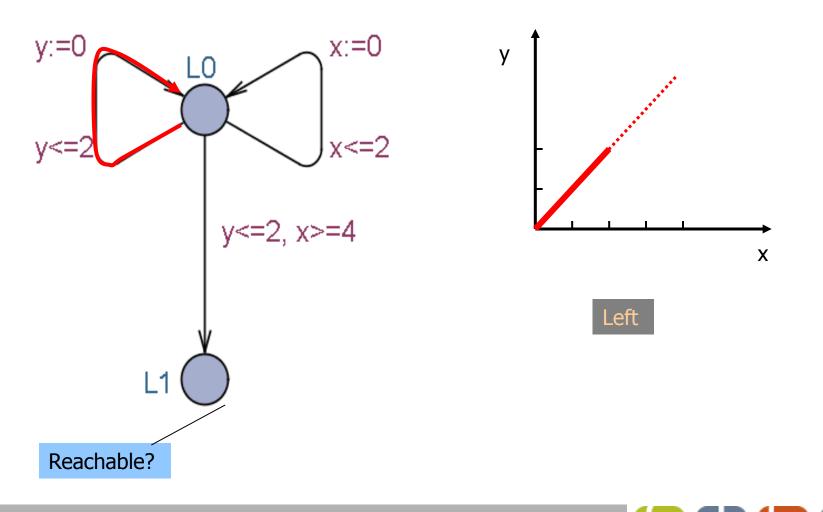
Kim Larsen [18]



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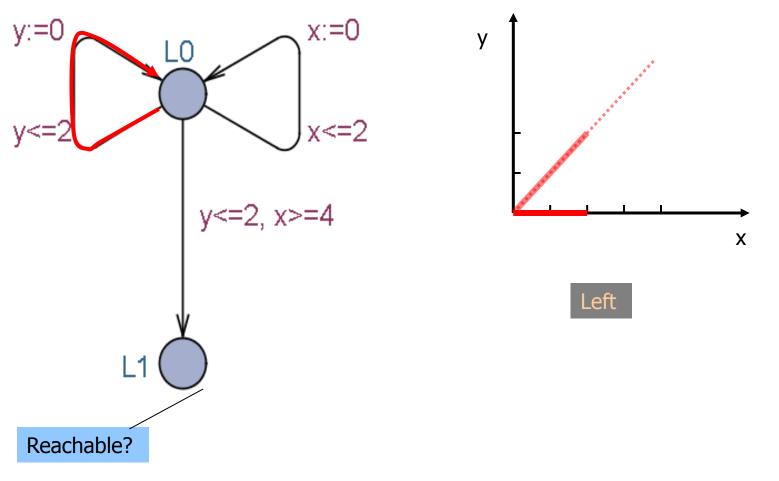
Kim Larsen [19]





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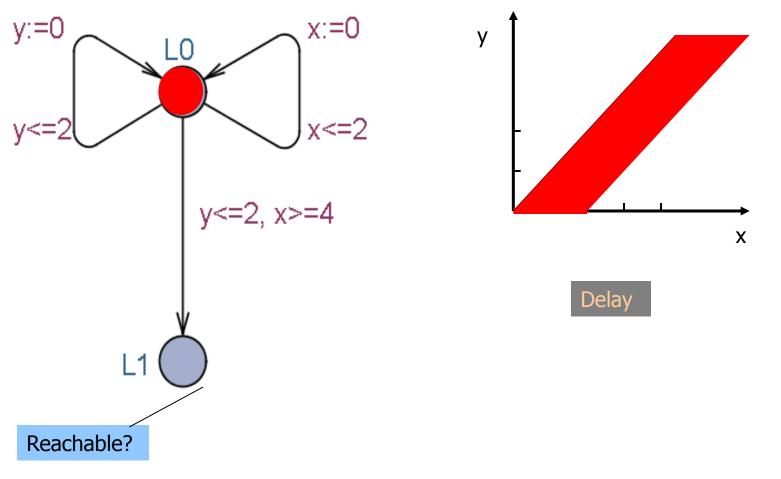
Kim Larsen [20]



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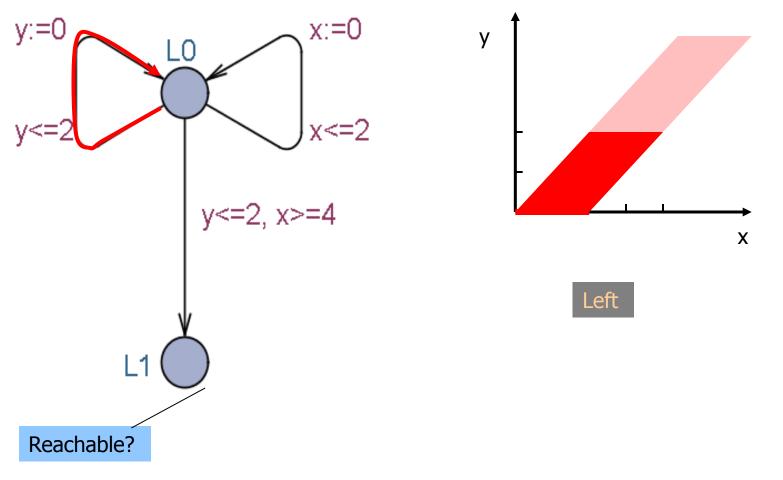
Kim Larsen [21]





Kim Larsen [22]

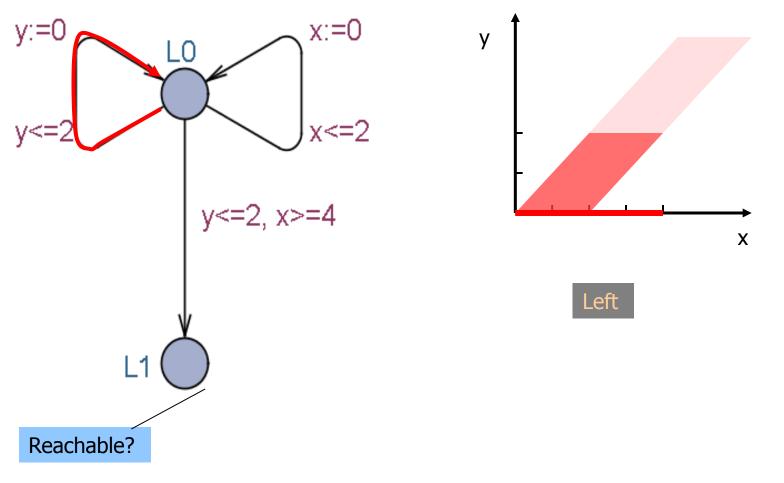




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Kim Larsen [23]

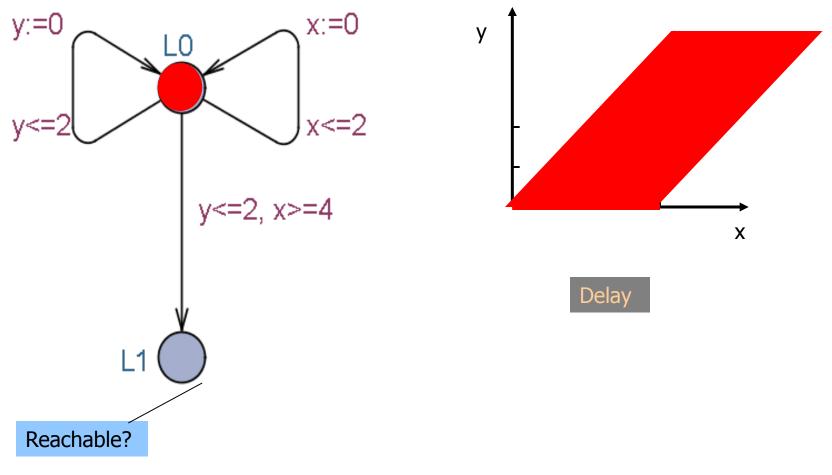




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Kim Larsen [24]

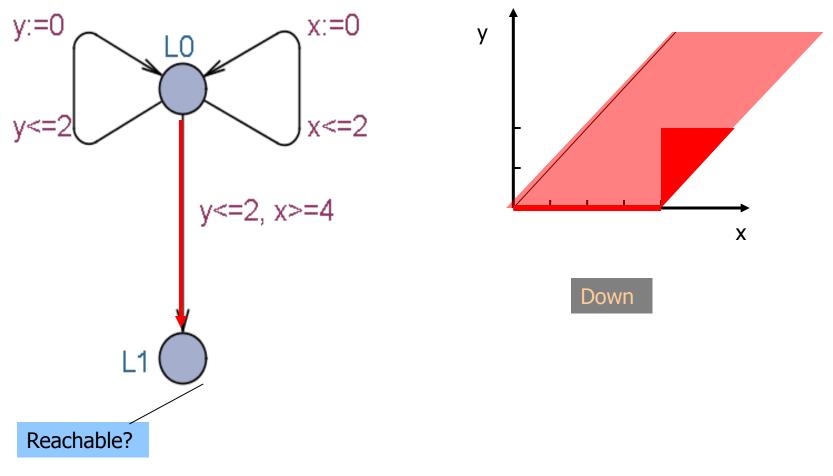




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Kim Larsen [25]





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Kim Larsen [26]

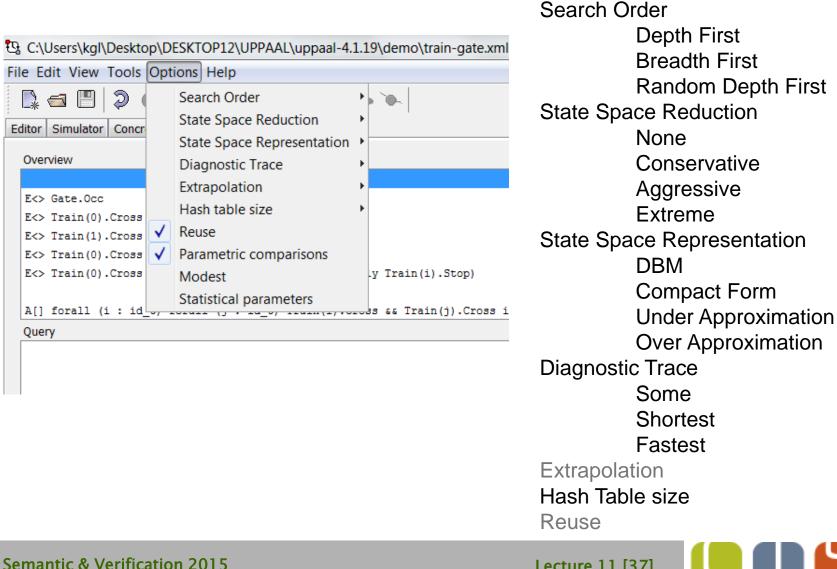


Verification Options



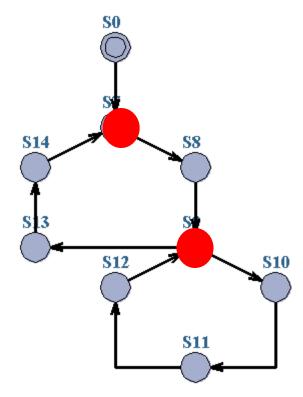


Verification Options



Lecture 11 [37]

State Space Reduction

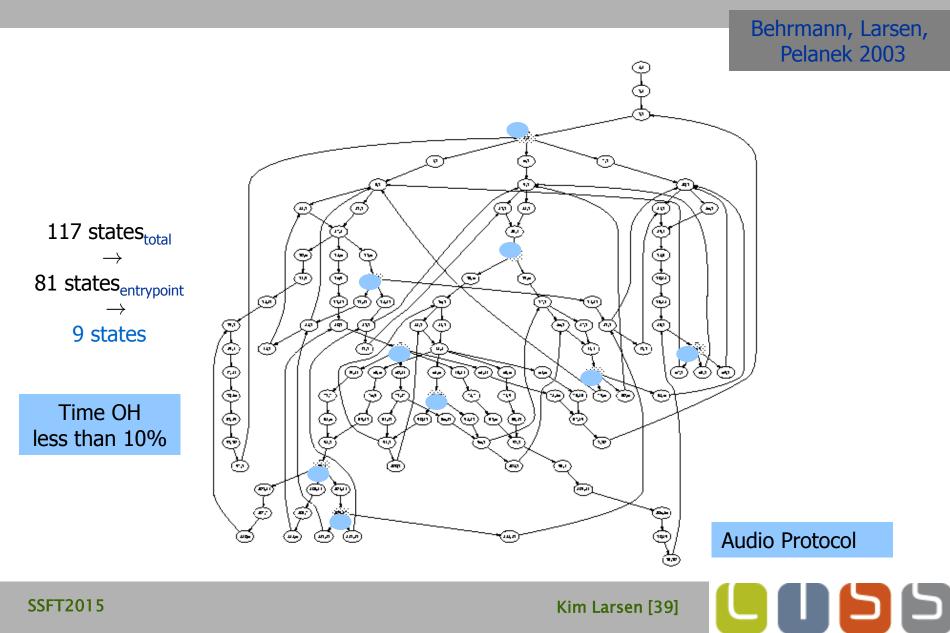


Cycles:

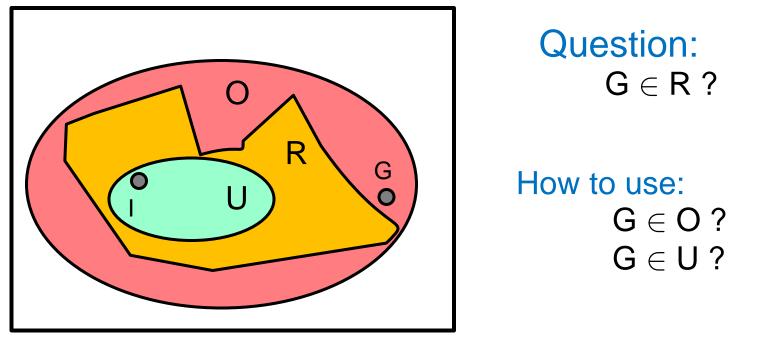
Only symbolic states involving loop-entry points need to be saved on Passed list



To Store or Not To Store



Over/Under Approximation



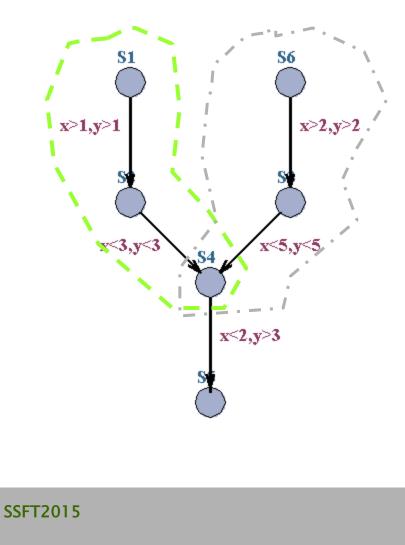
Declared State Space

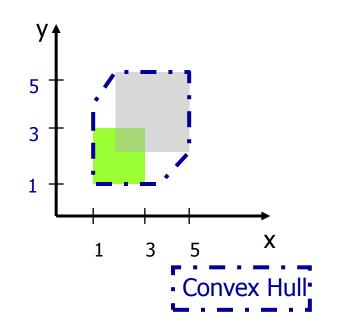
 $\begin{array}{l} G {\in U} \ \Rightarrow G {\in R} \\ \neg (G {\in O}) \Rightarrow \neg (G {\in R}) \end{array}$

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Kim Larsen [40]

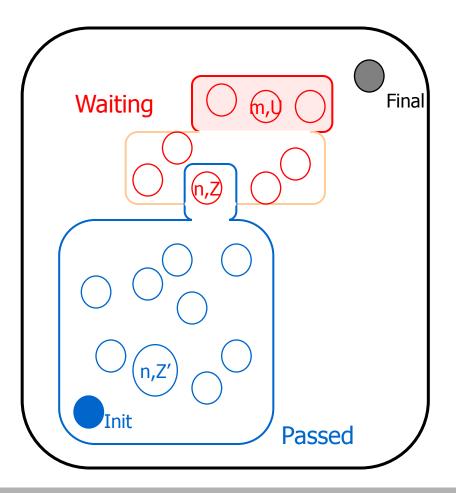
Over-approximation Convex Hull





TACAS04: An EXACT method performing as well as Convex Hull has been developed based on abstractions taking max constants into account distinguishing between clocks, locations and $\leq \& \geq$

Under-approximation Bitstate Hashing

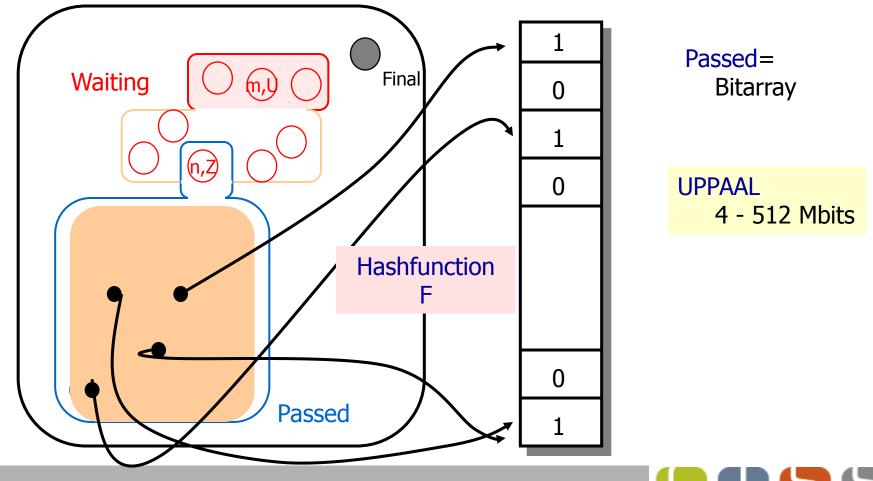




Kim Larsen [42]



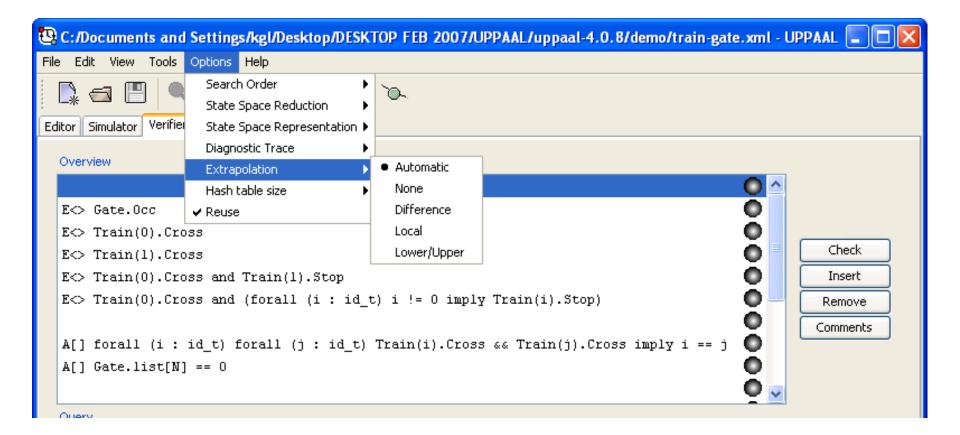
Under-approximation Bitstate Hashing



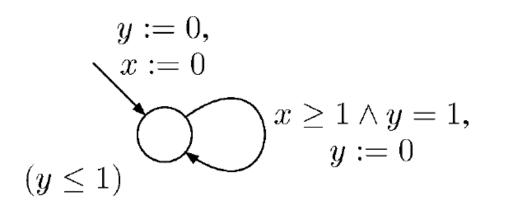
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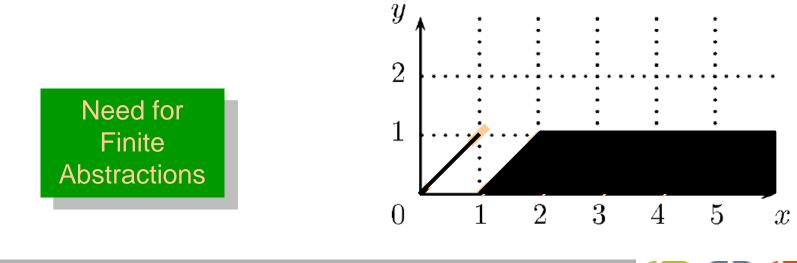
Extrapolation



Forward Symbolic Exploration







Kim Larsen [45]

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Abstractions

$$a: \mathcal{P}(R_{\geq 0}^X) \hookrightarrow \mathcal{P}(R_{\geq 0}^X)$$
 such that $W \subseteq a(W)$

$$\frac{(\ell, W) \Rightarrow (\ell', W')}{(\ell, W) \Rightarrow_{a} (\ell', a(W'))} \quad \text{if } W = a(W)$$

We want \Rightarrow_a to be:

- sound & complete wrt reachability
- finite
- easy to compute
- as coarse as possible

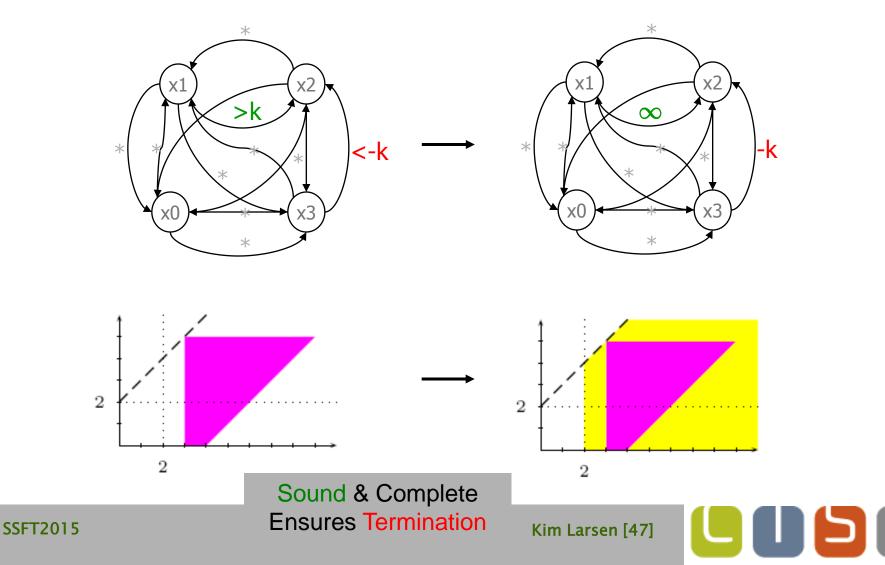
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Abstraction by Extrapolation

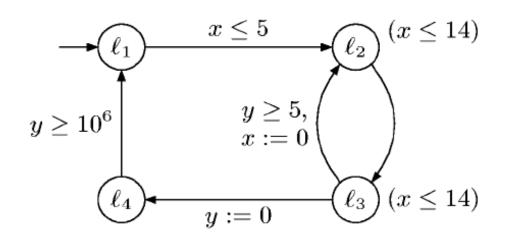
[Daws, Tripakis 98]

Let *k* be the largest constant appearing in the TA



Location Dependency

[Behrmann, Bouyer, Fleury, Larsen 03]



$$k_x = 5 k_y = 10^6$$

Will generate all symbolic states of the form

 $(I_2, x \in [0, 14], y \in [5, 14n], y - x \in [5, 14n - 14])$

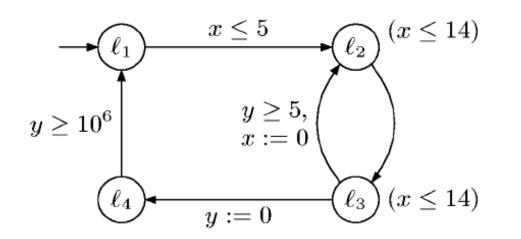
for $n \le 10^{6}/14 !!$

But $y \ge 10^6$ is not RELEVANT in I_2

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Location Dependent Constants



$$k_x = 5 \ k_y = 10^6$$

$$k_x^{i} = 14 \quad \text{for } i \in \{1, 2, 3, 4\}$$

$$k_y^{i} = 5 \quad \text{for } i \in \{1, 2, 3\}$$

$$k_y^4 = 10^6$$

 k_j^i may be found as solution to simple linear constraints!

Active Clock Reduction: $k_j^i = -\infty$

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Experiments

Active by default

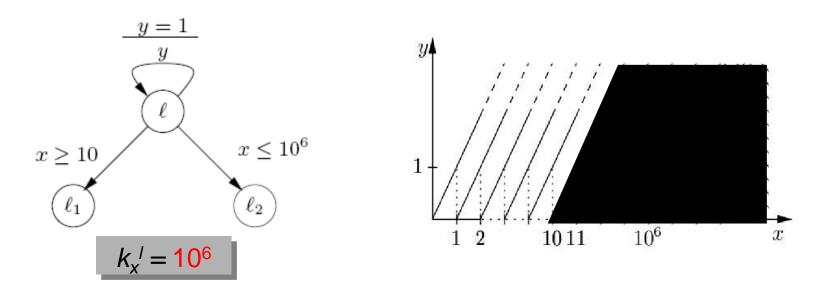
	Constant	Global	Active-clock	Local
	BIG	Method	Reduction	Constants
	10^{3}	0.05s/1MB	0.05s/1MB	0.00s/1MB
Naive Example	10^{4}	4.78s/3MB	4.83s/3MB	0.00s/1MB
Ivaive Example	10^{5}	484s/13MB	480s/13MB	0.00s/1MB
	10^{6}	stopped	stopped	0.00s/1MB
	10^{3}	3.24s/3MB	3.26s/3MB	0.01s/1MB
Two Processes	10^{4}	5981s/9MB	5978s/9MB	0.37s/2MB
	10^{5}	stopped	stopped	72s/5MB
	10^{3}	0.01s/1MB	0.01s/1MB	0.01s/1MB
Asymmetric	10^{4}	2.20s/3MB	2.20s/3MB	0.85s/2MB
Fischer	ischer 10^5 333		333s/19MB	160s/13MB
	10^{6}	33307s/122MB	33238s/122MB	16330s/65MB
Bang & Olufsen	25000	stopped	159s/243MB	123s/204MB

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Lower and Upper Bounds Behrmann, Bouyer, Larsen, Pelanek 04]



Given that $x \le 10^6$ is an *upper* bound implies that

 (I,v_x,v_y) simulates (I,v_x,v_y)

whenever $v'_x \ge v_x \ge 10$.

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For reachability downward closure wrt simulation Kim Larsen [51] suffices!

Advanced Extrapolation

		Classical		Loc. dep. Max		Loc. dep. LU		Convex Hull					
		-n1		-n2		-n3		-A					
Fischer	Model	Time	States	Mem	Time	States	Mem	Time	States	Mem	Time	States	Mem
	f5	4.02	82,685	5	0.24	16,980	3	0.03	2,870	3	0.03	3,650	3
	f6	597.04	1,489,230	49	6.67	158,220	7	0.11	11,484	3	0.10	14,658	3
	f7				352.67	1,620,542	46	0.47	44,142	3	0.45	56,252	5
sc	f8							2.11	164,528	6	2.08	208,744	12
ΪĒ	f9							8.76	598,662	19	9.11	754,974	39
CSMA/CD	f10							37.26	2,136,980	68	39.13	2,676,150	143
	f11							152.44	7,510,382	268			
	c5	0.55	27,174	3	0.14	10,569	3	0.02	2,027	3	0.03	1,651	3
	c6	19.39	287,109	11	3.63	87,977	5	0.10	6,296	3	0.06	4,986	3
	c7				195.35	813,924	29	0.28	18,205	3	0.22	14,101	4
٩Þ	c8							0.98	50,058	5	0.66	38,060	7
ູ່ດ	c9							2.90	132,623	12	1.89	99,215	17
0	c10							8.42	341,452	29	5.48	251,758	49
	c11							24.13	859,265	76	15.66	625,225	138
	c12							68.20	2,122,286	202	43.10	1,525,536	394
	bus	102.28	6,727,443	303	66.54	4,620,666	254	62.01	4,317,920	246	45.08	3,826,742	324
	philips	0.16	12,823	3	0.09	6,763	3	0.09	6,599	3	0.07	5,992	3
	sched	17.01	929,726	76	15.09	700,917	58	12.85	619,351	52	55.41	3,636,576	427

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Application: Schedulability Analysis

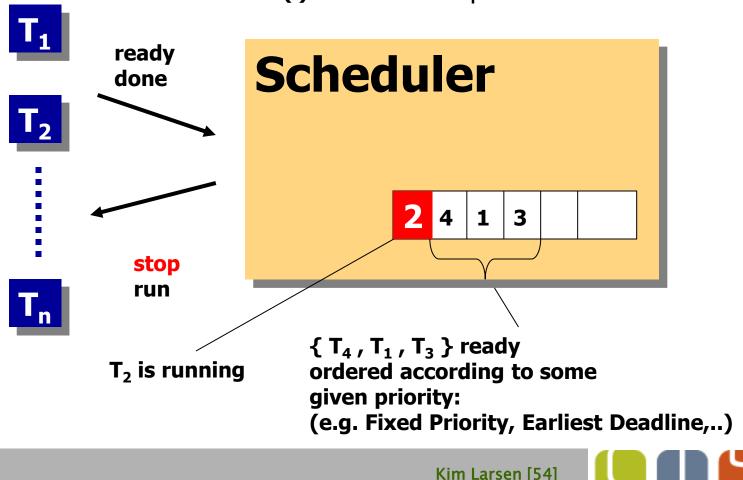




Task Scheduling

utilization of CPU

P(i), [E(i), L(i)], .. : period or earliest/latest arrival or .. for T_i C(i): execution time for T_i D(i): deadline for T_i



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Classical Scheduling Theory

Utilisation-Based Analysis

 A simple sufficient but not necessary schedulability test exists

$$U \equiv \sum_{i=1}^{N} \frac{C_i}{T_i} \le N(2^{1/N} - 1)$$

$$U \leq 0.69$$
 as $N \rightarrow \infty$

Where C is WCET and T is period

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Response Time Equation

$$R_{i} = C_{i} + \sum_{j \in hp(i)} \left\lceil \frac{R_{i}}{T_{j}} \right\rceil C_{j}$$

Where hp(i) is the set of tasks with priority higher than task i

Solve by forming a recurrence relationship:

$$w_i^{n+1} = C_i + \sum_{j \in hp(i)} \left| \frac{w_i^n}{T_j} \right| C_j$$

The set of values $w_i^0, w_i^1, w_i^2, ..., w_i^n, ...$ is monotonically non decreasing When $w_i^n = w_i^{n+1}$ the solution to the equation has been found, w_i^0 must not be greater that R_i (e.g. 0 or C_i)

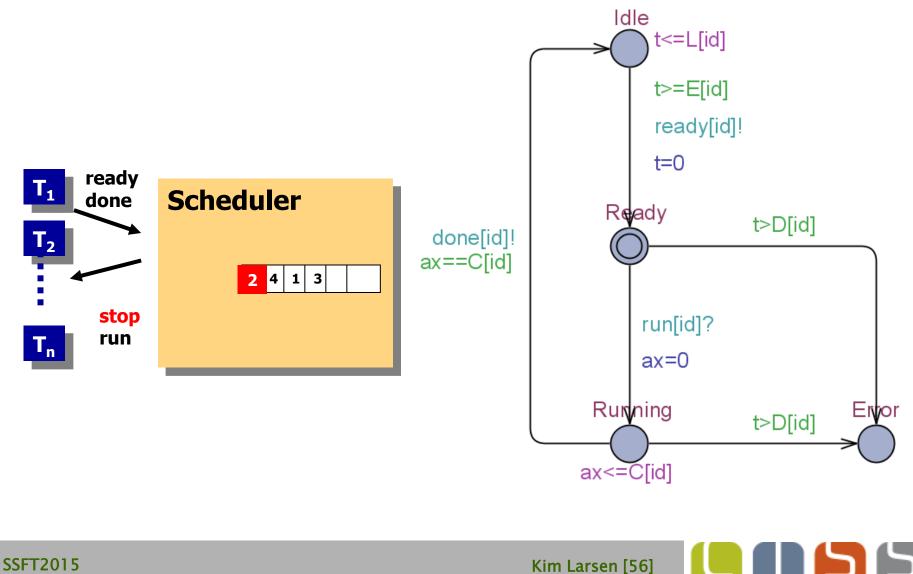
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✓ Simple to perform

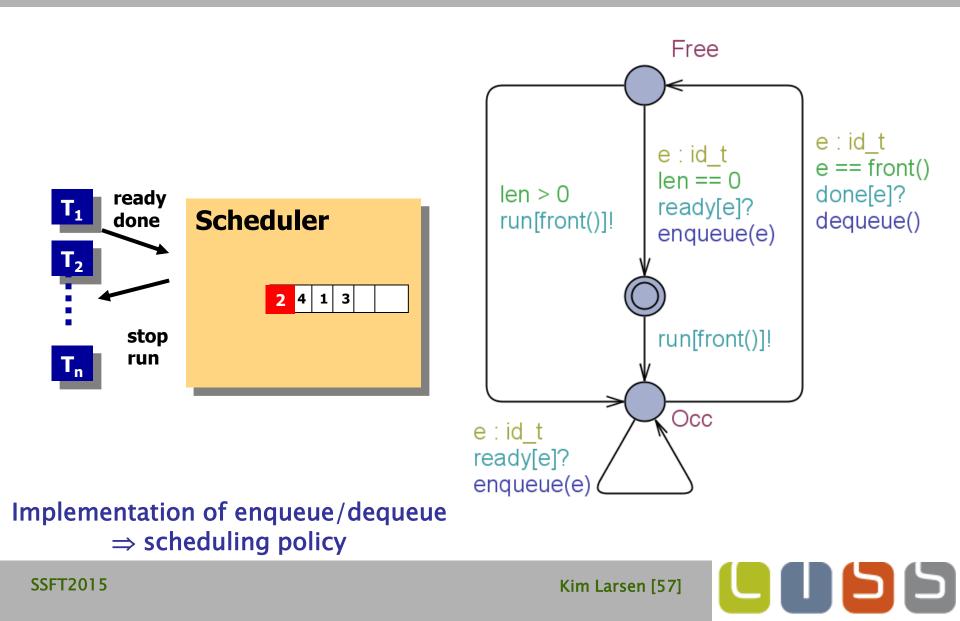
- Overly conservative
- Limited settings
- Single-processor
- \Rightarrow Do it in UPPAAL!

Kim Larsen [55]

Modeling Task

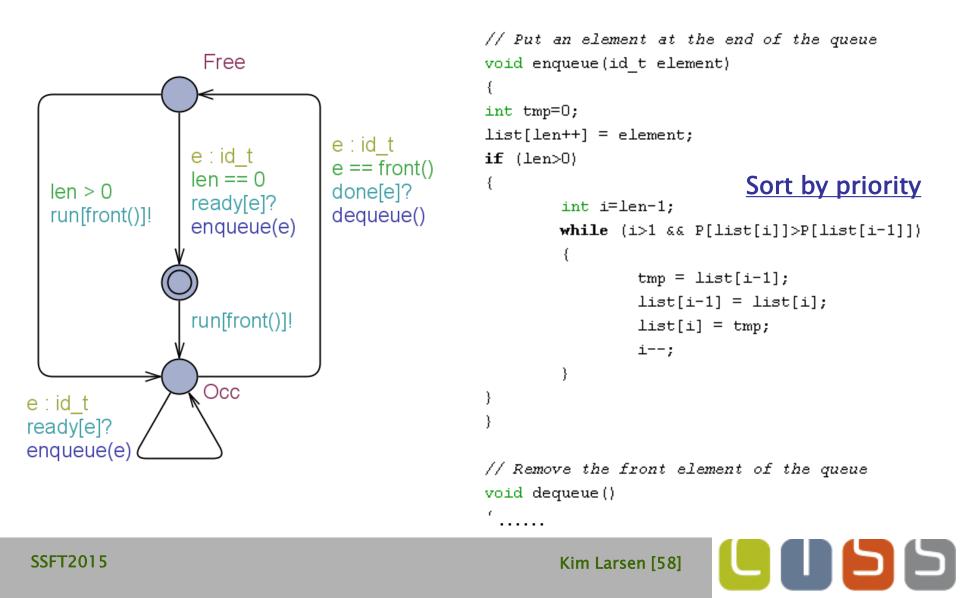


Modeling Scheduler

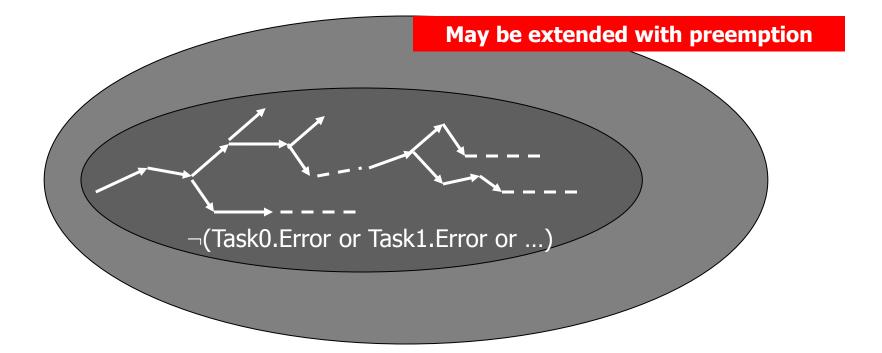


Modeling Queue

In UPPAAL 4.0 User Defined Function



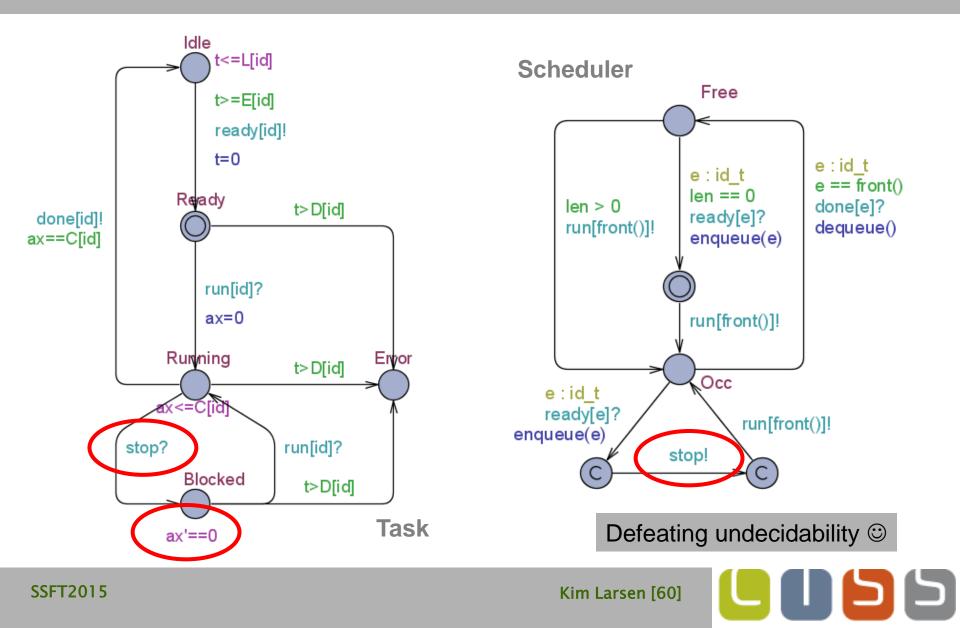
Schedulability = Safety Property



A□ ¬(Task0.Error or Task1.Error or ...)



Preemption – Stopwatches!



LAB-Exercises (cont)

http://people.cs.aau.dk/~kgl/Shanghai2013/

Exercise 1 (Brick Sorter) Exercise 2 (Coffee Machine) Excercise 19 (Train Crossing) Exercise 28 (Jobshop Scheduling) Exercise 14 (Gossiping Girls)

