



The elements to sort (actually used for comparisons) are also called the keys.



You should know these complexities from a previous course on algorithms.



We assume internal sorting is possible.



We assume comparison based sorting is used.

















Example: <1,2,4,7,6,0> & <8,9,2,1,0,4> are bitonic sequences.





And in fact the procedure works even if the original sequence needs a cyclic shift to look like this particular case.



Cost:  $\Theta(\log n)$  obviously.



Bitonic Sort
Wires
$\begin{array}{c} 0000\\0001\\0001\\0010\\0011\\0011\\0001\\000$
Cost: O(log <sup>2</sup> n).
Simulated on a serial computer: $O(n \log^2 n)$ .
$\begin{array}{c c} 1001 & \oplus BM[2] \\ 1010 \\ 1011 & \oplus BM[2] \\ \end{array} \oplus BM[4] \\ \oplus BM[6] \\ \end{array}$
$\begin{array}{c} 1100\\ 1101\\ 1110\\ 11111\\ 1111\\ 1111\\ 1111\\ 11111\\ 1111\\ 1111\\ 1111\\ 1111\\ 1111\\ 1111\\ 1111\\ 1111\\ 1111\\ 1111\\ 111$

Not cost optimal compared to the optimal serial algorithm.



Hypercube: Neighbors differ with each other by one bit.



It is difficult to sort n elements in time logn using n processes (cost optimal w.r.t. the best serial algorithm in  $n \log n$ ) but it is easy to parallelize other (less efficient) algorithms.







Write speedup & efficiency to find the bound on p but you can also see it with  $T_{P}$ .











Hoare partitioning is better. Check in your algorithm course.











This algorithm does not correspond exactly to the serial version. Time for partitioning: O(1).















