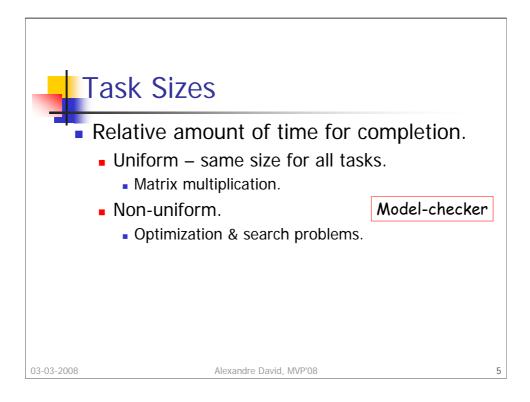
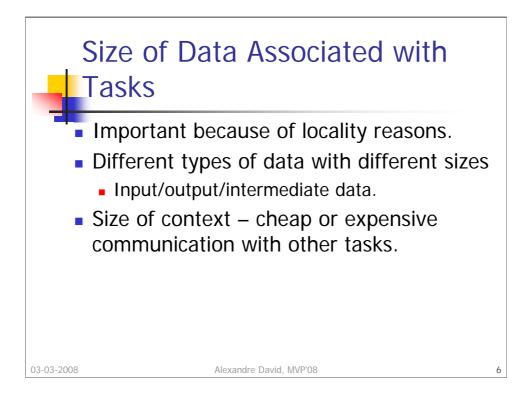


The well-structured problem can typically be decomposed using data or recursive decomposition techniques.

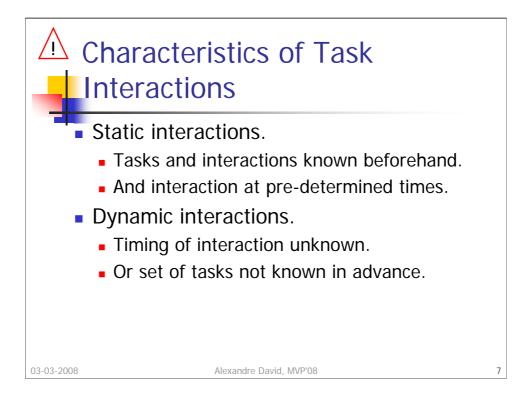
Dynamic tasks generation: Exploratory or speculative decomposition techniques are generally used, but not always. Example: quicksort.



Typically the size of non-uniform tasks is difficult to evaluate beforehand.



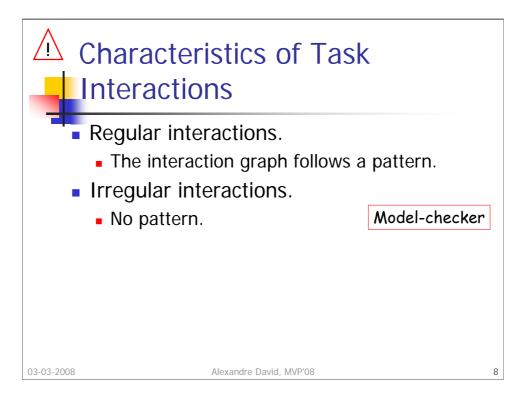
Example of 15-puzzle has a small context: easy to communicate the tasks to different processes.



Static vs. dynamic.

Static or dynamic interaction pattern.

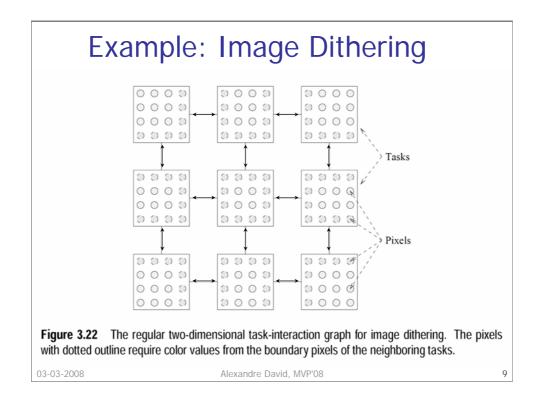
Dynamic harder to code, more difficult for MPI.



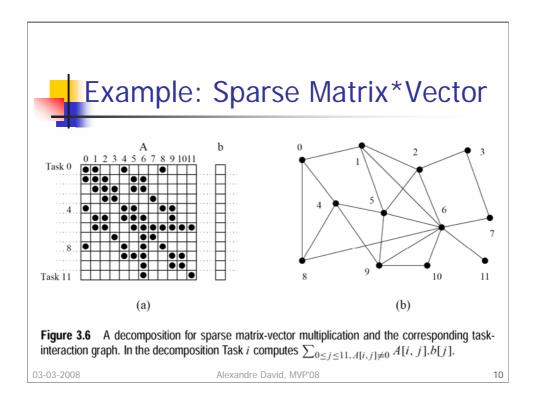
Regular vs. irregular.

Regular patterns can be exploited for efficient implementations.

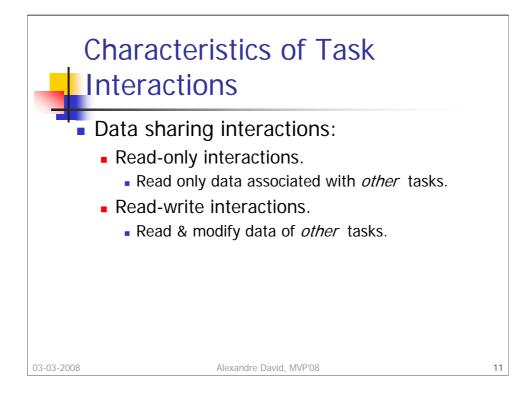
Dynamic harder to code, more difficult for MPI.



The color of each pixel is determined as the weighted average of its original value and the values of the neighboring pixels. Decompose into regions, 1 task/region. Pattern is a 2-D mesh. Regular pattern.

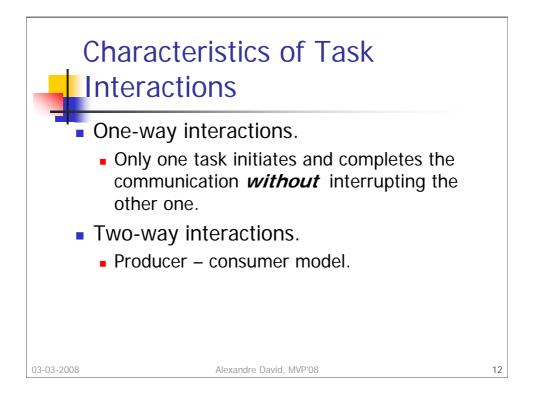


Irregular pattern. Interaction pattern depends on the values in A.



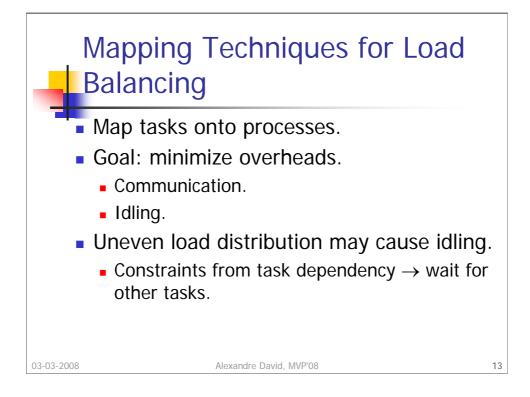
Read-only vs. read-write.

Read-only example: matrix multiplication (share input). Read-write example: 15-puzzle with shared priority list of states to be explored; Priority given by some heuristic to evaluate the distance to the goal.



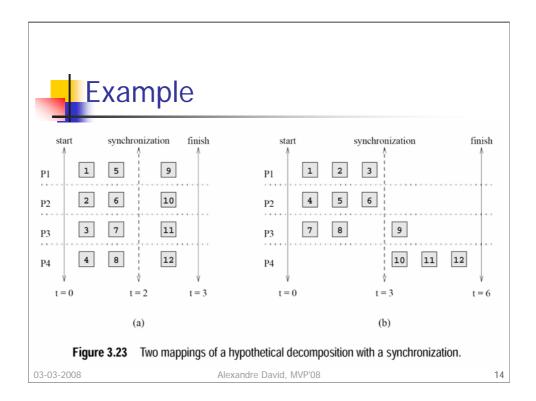
One-way vs. two-way.

One-way more difficult with MPI since MPI has an explicit send & receive set of calls. Conversion one-way to two-way with polling or another thread waiting for communication.

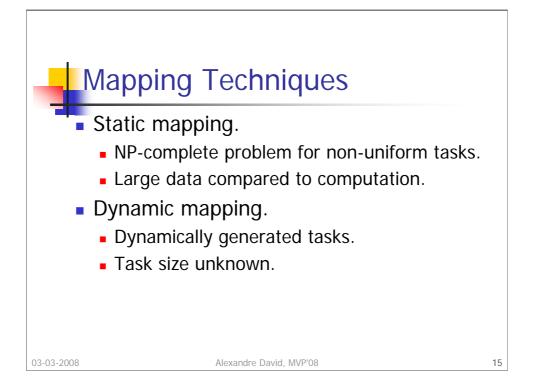


Minimizing communication may contradict minimizing idling. Put tasks that communicate with each other on the same process but may unbalance the load -> distribute them but increase communication.

Load balancing is not enough to minimize idling.



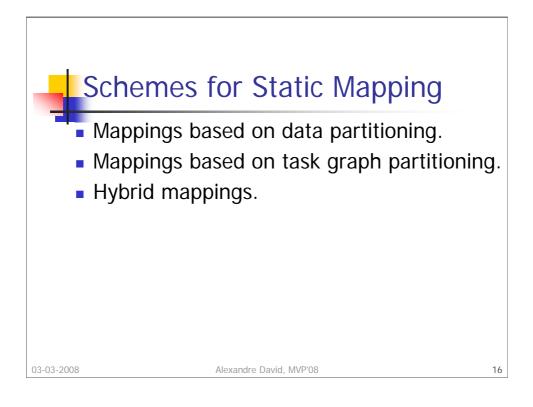
Global balancing OK but due to task dependency P4 is idling.

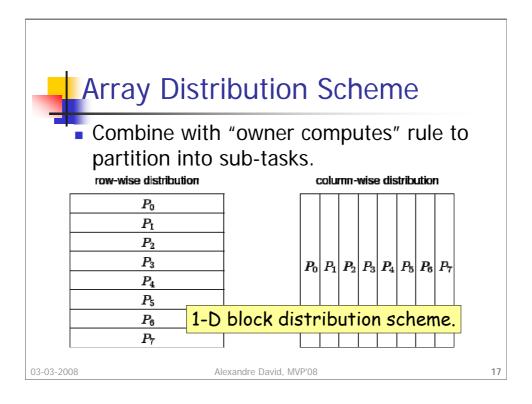


Even static mapping may be difficult: The problem of obtaining an optimal mapping is an NP-complete problem for non-uniform tasks. In practice simple heuristics provide good mappings.

Cost of moving data may out-weight the advantages of dynamic mapping.

In shared address space dynamic mapping may work well even with large data, but be careful with the underlying architecture (NUMA/UMA) because data may be moved physically.

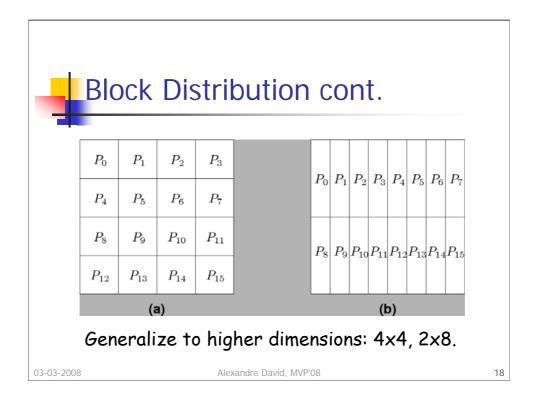


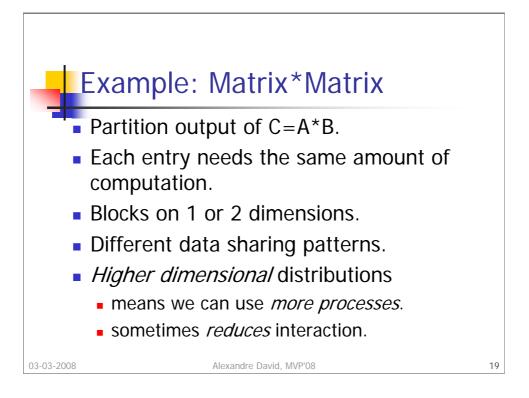


Data partitioning mapping.

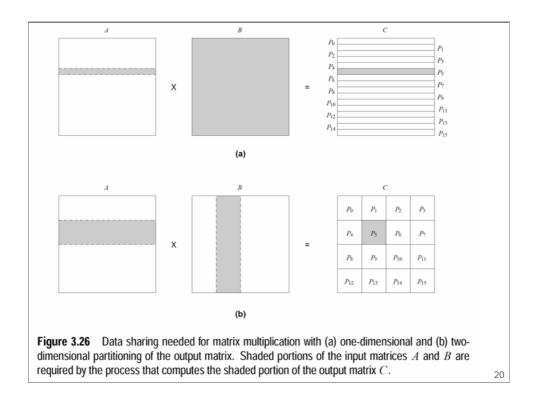
Mapping data = mapping tasks.

Simple block-distribution.

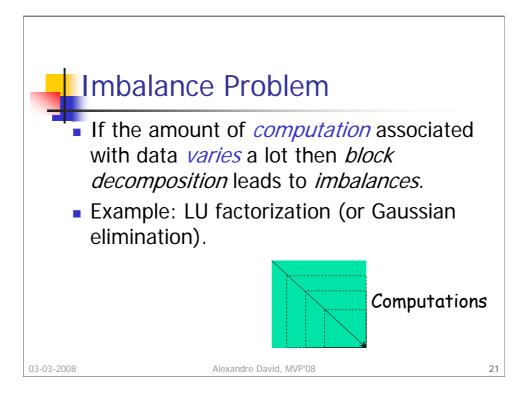




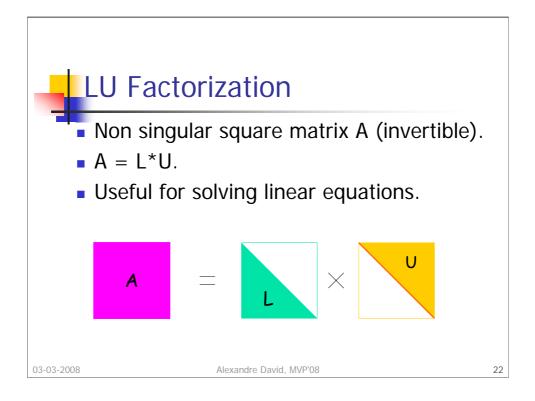
In the case of matrix n*n multiplication, 1-D -> n processes at most, 2-D n^2 processes at most.

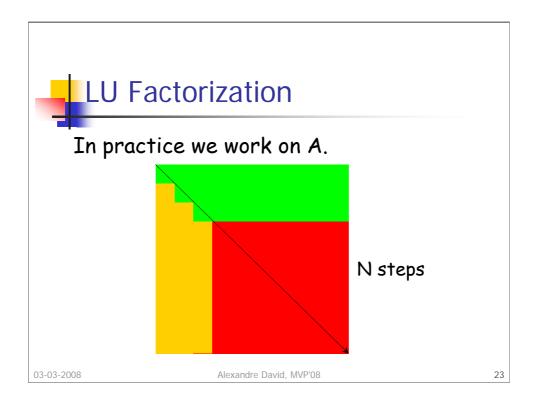


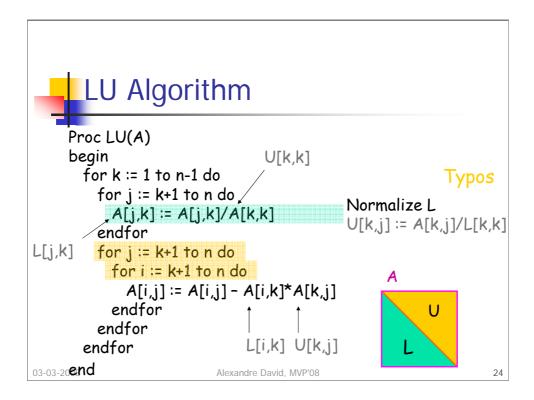
 $O(n^2/sqrt(p))$ vs. $O(n^2)$ shared data.

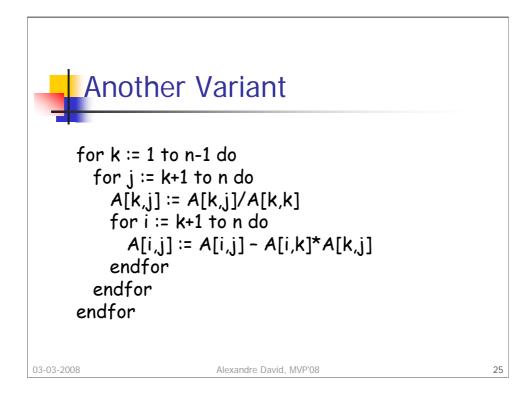


Exercise on LU-decomposition.

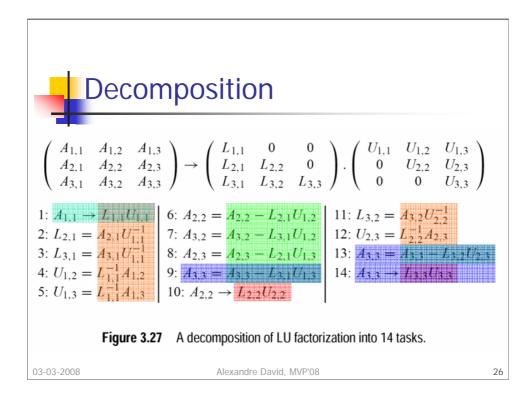




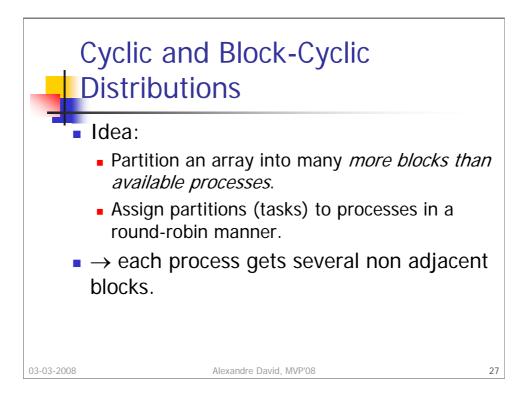


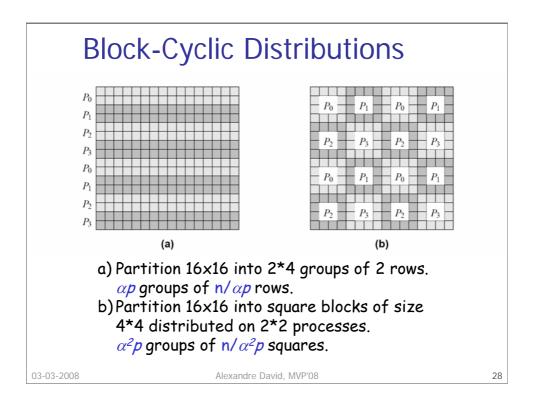


More common in the litterature.



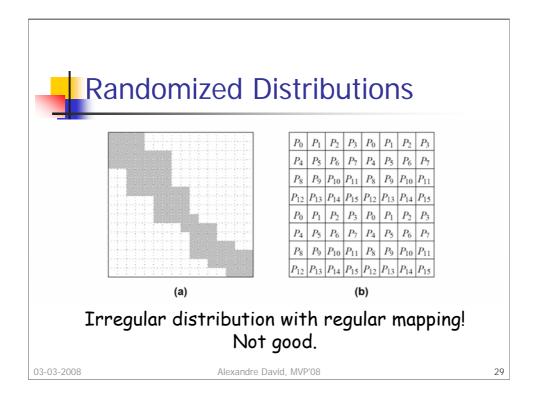
Load imbalance for individual tasks. Load imbalance from dependencies.

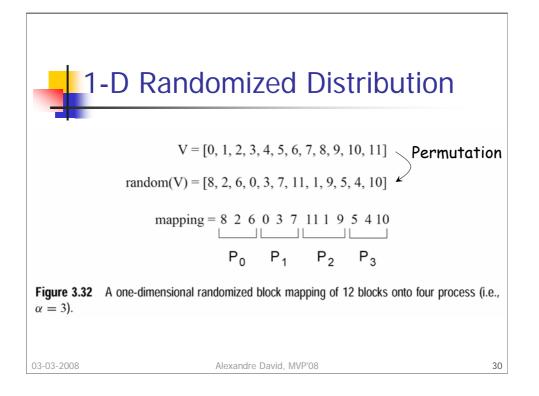


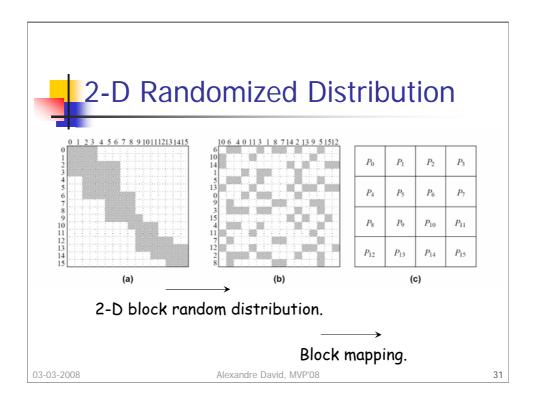


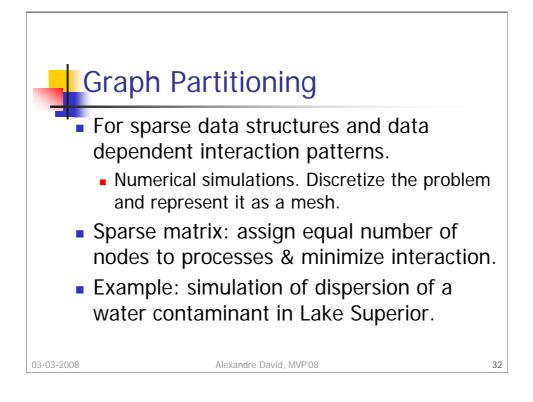
Reduce the amount of idling because all processes have a sampling of tasks from *all parts* of the matrix.

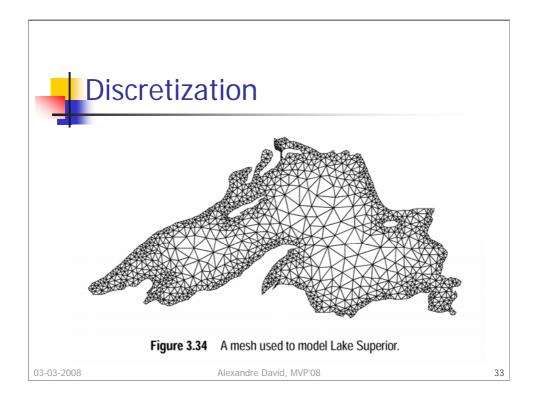
But lack of locality may result in performance penalties + leads to high degree of interaction. Good value for α to find a compromise.

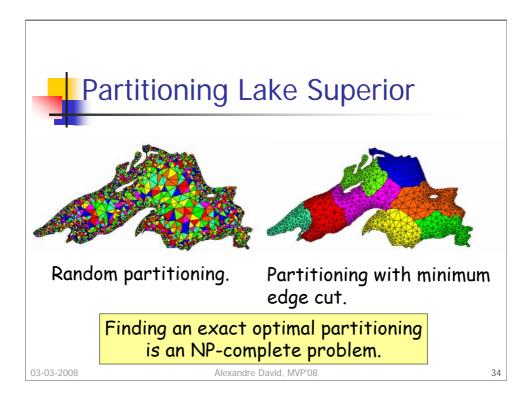




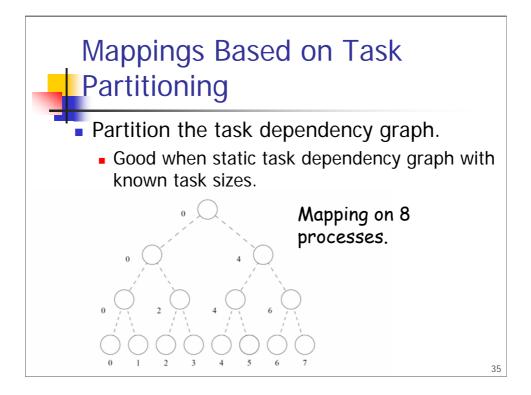








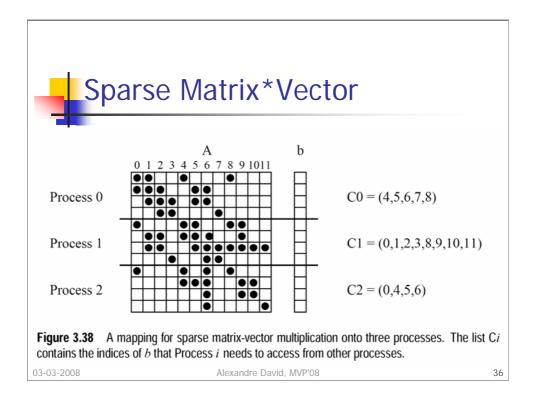
Minimum edge cut from a graph point of view. Keep locality of data with processes to minimize interaction.



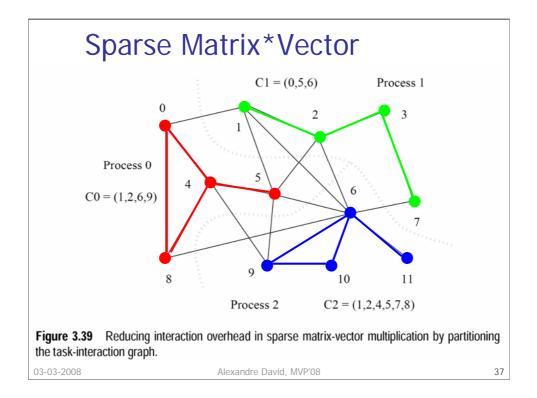
Determining an optimal mapping is NP-complete. Good heuristics for structured graphs.

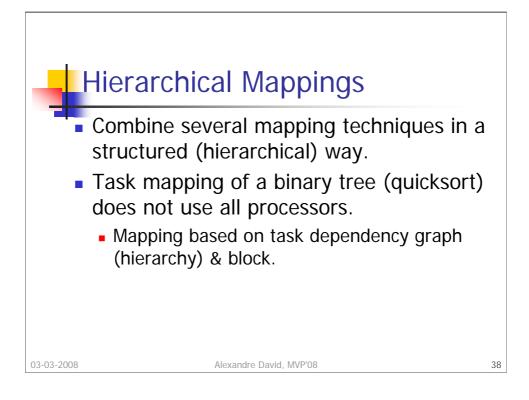
Binary tree task dependency graph: occurs in recursive decompositions as seen before. The mapping minimizes interaction. There is idling but it is inherent to the task dependency graph, we do not add more.

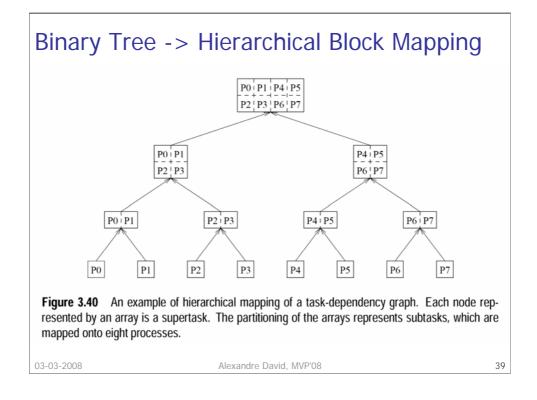
This example good on a hypercube. See why?

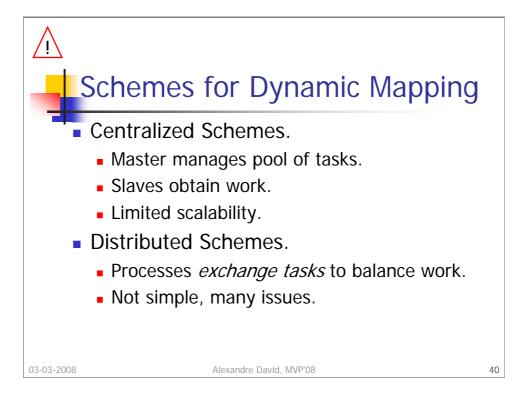


Example seen before.









Centralized schemes are easy to implement but present an obvious bottleneck (the master).

Self-scheduling: slaves pick up work to do whenever they are idle.

Bottleneck: tasks of size M, it takes t to assign work to a slave \rightarrow at most M/t processes can be kept busy.

Chunk-scheduling: a way to reduce bottlenecks by getting a group of tasks. Problem for load imbalances.

Distributed schemes more difficult to implement.

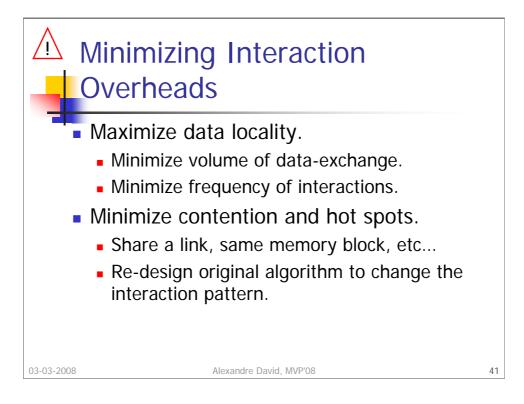
How do you choose sender & receiver? i.e. if A is overloaded, which process gets something?

Initiate transfer by sender or receiver? i.e. A overloaded sends work or B idle requests work?

How much work to transfer?

When to transfer?

Answers are application specific.

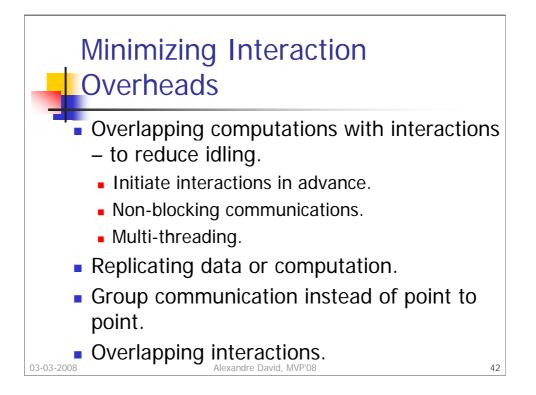


Minimize volume of exchange \rightarrow maximize temporal locality. Use higher dimensional distributions, like in the matrix multiplication example. We can store intermediate results and update global results less often.

Minimize frequency of interactions \rightarrow maximize spatial locality.

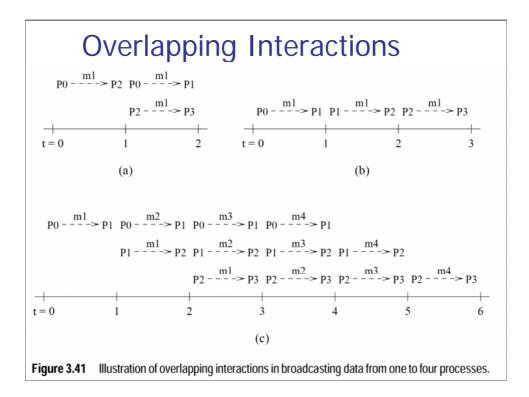
Related to the previously seen cost model for communications.

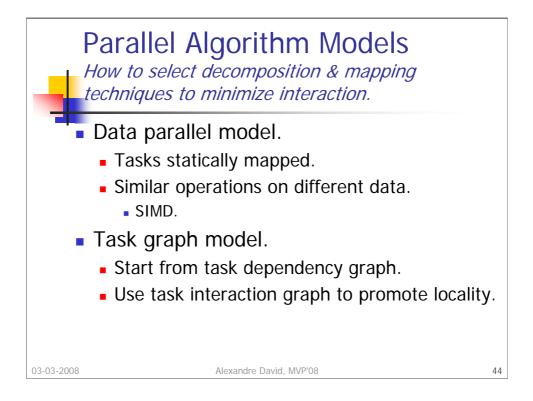
Changing the interaction pattern: For the matrix multiplication example, the sum is commutative so we can re-order the operations modulo sqrt(p) to remove contention.



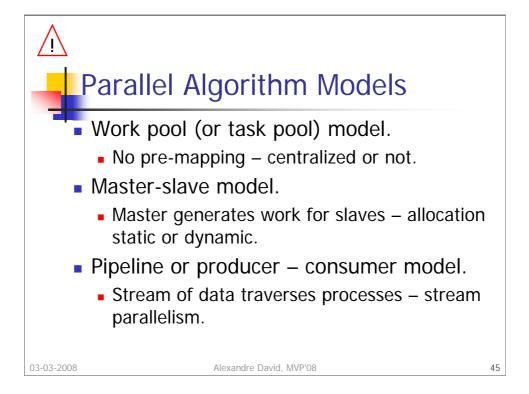
Replication is useful when the cost of interaction is greater than replicating the computation. Replicating data is like caching, good for read-only accesses. Processing power is cheap, memory access is expensive – also apply at larger scale with communicating processes.

Collective communication such as broadcast. However, depending on the communication pattern, a custom collective communication may be better.





An algorithm model is a *way of structuring a parallel algorithm* by selecting a *decomposition and mapping* technique and applying the appropriate strategy to minimize interactions.



Pipeline model heavily used in GPUs. Load balancing is a function of task granularity.

- + hybrid models:
- •Multiple models applied hierarchically.
- •Multiple models applied sequentially to different phases.